

Name:

Course: CAP 4601

Semester: Summer 2013

Assignment: Assignment 2

Date: 03 JUN 2013

Complete the following written problems:

1. (10 Points) Given that a loaded coin has the following probability for coming up heads:

$P(\text{Loaded Coin} = \text{heads}) = 0.25$. What is the probability that the loaded coin will come up tails?

In other words, what is $P(\text{Loaded Coin} = \text{tails})$?

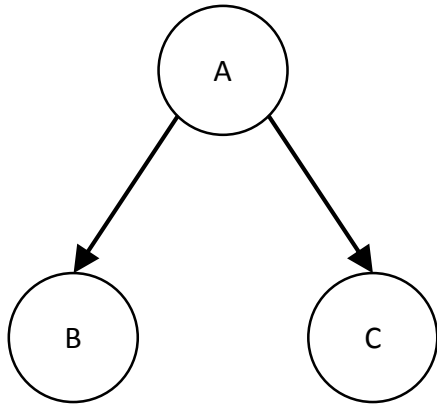
2. (20 Points) Given loaded coin tosses are independent events and that a different loaded coin has the following probability for coming up heads twice in a row:

$P(\text{Loaded Coin} = \text{heads}, \text{Loaded Coin} = \text{heads}) = 0.16$. What is the probability that the loaded coin will come up tails twice in a row? In other words, what is

$P(\text{Loaded Coin} = \text{tails}, \text{Loaded Coin} = \text{tails})$?

3. (40 Points) Given a fair coin with $P(\text{Fair Coin} = \text{heads}) = 0.5$ and a loaded coin with $P(\text{Loaded Coin} = \text{heads}) = 1$, if we pick a coin at random (i.e. $P(\text{Choice} = \text{Fair Coin}) = P(\text{Choice} = \text{Loaded Coin}) = 0.5$) and flip it, what is the probability that it is the loaded coin given that we observe heads? In other words, what is $P(\text{Choice} = \text{Loaded Coin} | \text{Coin} = \text{heads})$?

4. (40 Points) Given the following Bayes Network:



With the following probabilities:

$$P(A) = 0.5$$

$$P(B|A) = 0.2$$

$$P(B|\neg A) = 0.2$$

$$P(C|A) = 0.8$$

$$P(C|\neg A) = 0.4$$

- What is $P(B|C)$?

- What is $P(C|B)$?

5. (130 Points) Using the data below, construct a Naïve Bayesian Network that does **NOT** use Laplacian Smoothing to predict that an [Iris](#) is an [Iris versicolor](#) based on if its sepals are long or wide.

Note: [Sepals](#) are the green petal-like objects surrounding a flower.

Long Sepals	Wide Sepals	Iris versicolor
false	true	false
false	false	false
false	true	false
false	true	false
false	true	false
false	true	false
false	true	false
false	true	false
false	false	false
false	true	false
true	true	true
true	true	true
true	true	true
true	false	true
true	false	true
true	false	true
true	true	true
false	false	true
true	false	true
false	false	true

Do the following:

- Draw the graph of the Naïve Bayesian Network.

- Given the data above, answer the following questions:

a. What is the probability that an Iris is an Iris versicolor? In other words, what is

$P(\text{Iris versicolor} = \text{true})$?

b. Given an Iris versicolor, what is the probability that its sepals are long? In other words, what is

$P(\text{Long Sepals} = \text{true} | \text{Iris versicolor} = \text{true})$?

c. Given an Iris versicolor, what is the probability that its sepals are wide? In other words, what

is $P(\text{Wide Sepals} = \text{true} | \text{Iris versicolor} = \text{true})$?

d. Given an Iris versicolor, what is the probability that its sepals are both long and wide? In other

words, what is $P(\text{Long Sepals} = \text{true}, \text{Wide Sepals} = \text{true} | \text{Iris versicolor} = \text{true})$?

e. Given an Iris that is not an Iris versicolor, what is the probability that its sepals are both long and wide? In other words, what is

$P(\text{Long Sepals} = \text{true}, \text{Wide Sepals} = \text{true} | \text{Iris versicolor} = \text{false})$?

f. Given an Iris with both long and wide sepals, what is the probability that it's an Iris versicolor?

In other words, what is $P(\text{Iris versicolor} = \text{true} | \text{Long Sepals} = \text{true}, \text{Wide Sepals} = \text{true})$?

6. (60 Points) Using the data from the previous problem, construct a Naïve Bayesian Network that **DOES** use Laplacian Smoothing to predict that an Iris is an Iris versicolor based on if its sepals are long or wide.

For Laplacian Smoothing, use $k = 1$.

- Given the data above, answer the following questions:

a. What is the probability that an Iris is an Iris versicolor? In other words, what is $P(\text{Iris versicolor} = \text{true})$?

b. Given an Iris versicolor, what is the probability that its sepals are long? In other words, what is $P(\text{Long Sepals} = \text{true} | \text{Iris versicolor} = \text{true})$?

c. Given an Iris versicolor, what is the probability that its sepals are wide? In other words, what is $P(\text{Wide Sepals} = \text{true} | \text{Iris versicolor} = \text{true})$?

d. Given an Iris versicolor, what is the probability that its sepals are both long and wide? In other words, what is $P(\text{Long Sepals} = \text{true}, \text{Wide Sepals} = \text{true} | \text{Iris versicolor} = \text{true})$?

e. Given an Iris that is not an Iris versicolor, what is the probability that its sepals are both long and wide? In other words, what is $P(\text{Long Sepals} = \text{true}, \text{Wide Sepals} = \text{true} | \text{Iris versicolor} = \text{false})$?

f. Given an Iris with both long and wide sepals, what is the probability that it's an Iris versicolor?
In other words, what is $P(\text{Iris versicolor} = \text{true} | \text{Long Sepals} = \text{true}, \text{Wide Sepals} = \text{true})$?

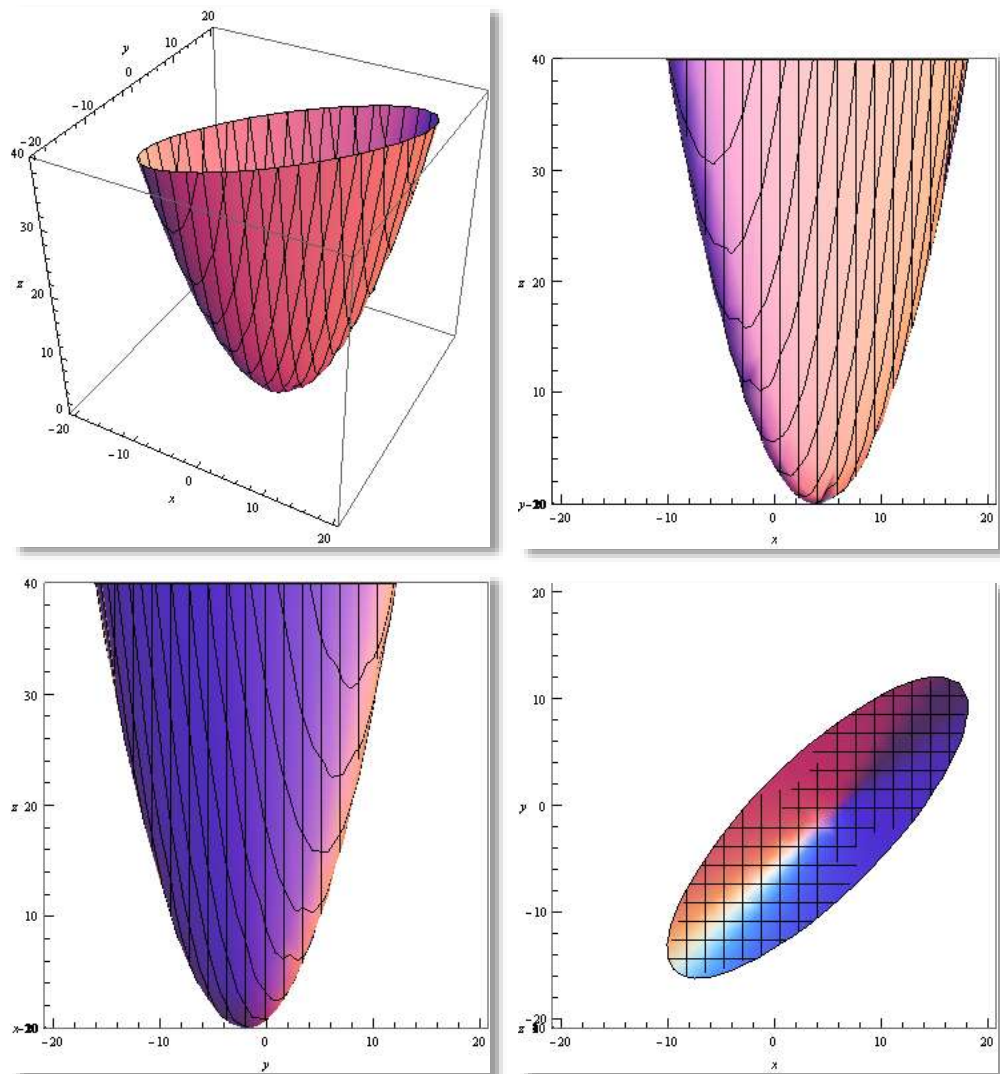
Complete the following programming problem on `linprog4.cs.fsu.edu`:

Download the ZIP file containing the directory structure and files for this programming problem:
[assignment 02.zip](#)

1. (100 Points) Use the method of gradient descent to find the minimum of a function.

Given the function:
$$f(x, y) = \frac{5x^2}{9} - \frac{8xy}{9} - \frac{56x}{9} + \frac{5y^2}{9} + \frac{52y}{9} + \frac{164}{9}$$

With the following plots:



Use the method of [gradient descent](#) to find the (x, y) value that produces the minimum $z = f(x, y)$ when we start [gradient descent](#) from $(0, 0)$ and use the learning rate $\alpha = 0.1$.

The [gradient descent](#) update formula is: $\mathbf{x}_{n+1} \leftarrow \mathbf{x}_n - \alpha \nabla f(\mathbf{x}_n)$; therefore, it is $(x_{n+1}, y_{n+1}) \leftarrow (x_n, y_n) - \alpha \nabla f(x_n, y_n)$ for this problem.

Stop the [gradient descent](#) when either:

- The difference in consecutive \mathbf{x}_i values is less than 0.000001. In other words, when $\|\mathbf{x}_{n+1} - \mathbf{x}_n\| < 0.000001$.
- The number of full [gradient descent](#) iterations exceeds 1024. In other words, don't do more than 1024 updates of gradient descent.

Use the following files:

- [print.hpp](#): The file containing operator `<<` to print arrays and `std::vector`.
- [main.cpp](#): The file for editing.
- [makefile](#): The makefile for `linprog4.cs.fsu.edu`.

Do not make changes to the `makefile`. Only make changes to `main.cpp`.

Use `std::cout` to output information exactly in the following format:

```
1: ( 0, 0 )
2: ( 0.622222, -0.577778 )
3: ( 1.12395, -1.03605 )
.
.
.
```

Note: The ellipses above should not be included in your output. The ellipses represent the rest of your properly formatted output for this [gradient descent](#) problem.

After completing Assignment 02, create an `assignment_02_lastname.pdf` file for your written assignment and an `assignment_02_lastname.zip` file for your programming assignment (where *lastname* is your last name). Ensure that your `assignment_02_lastname.zip` retains the directory structure of the original zip file. In other words, ensure your zip file has the following directory structure:

- /
 - o `gradient_descent/`
 - `print.hpp`
 - `main.cpp`
 - `makefile`

Upload both your `assignment_02_lastname.pdf` file for your written assignment and your `assignment_02_lastname.zip` file for your programming assignment to the Assignment 02 location on the [BlackBoard](https://campus.fsu.edu) site: <https://campus.fsu.edu>.