## **COP 5405: Advanced Algorithms**

Fall 2006

Lecture 20

## Layered range trees

We discuss a 2-dimensional layered range tree. Note that  $P(leftchild(v)) \subseteq P(v)$  and  $P(rightchild(v)) \subseteq P(v)$ . So the fractional cascading idea can be used.

- The main tree is a balanced BST on the x coordinates.
- The associated data structure for node v in the above tree is a sorted array.
  - o The array is sorted on the *y* coordinates.
  - $\circ$  Each array element stores two pointers, one to an array element in the associated data structure of leftchild(v), and one to an array element in the associated data structure of rightchild(v), based on the fractional cascading idea.
- A *d*-dimensional layered range tree can be constructed in time  $O(n \log^{d-1} n)$  time and uses  $O(n \log^{d-1} n)$  storage,  $d \ge 2$ .

A 2-dimensional range tree is queried as in 2-dimensional range tree, except that the 1-dimensional search is performed as follows.

- For array associated with  $v_{split}$ , perform binary search to find the location i corresponding to y.
- At a lower level node, find the location pointed to by  $A[v_{split}](i)$ .
- Repeatedly follow subsequent pointers at lower levels too.
- Query time is  $O(\log^{d-1} n + k)$  to report k points,  $d \ge 2$ .