COMMUNICATION CHARACTERISTICS IN THE NAS PARALLEL BENCHMARKS

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In this research, we investigate the communication characteristics of the Message Passing Interface (MPI) implementation of the NAS parallel benchmarks and study the feasibility and effectiveness of *compiled communication* on MPI programs. Compiled communication is a technique that utilizes the compiler knowledge of both the application communication requirement and the underlying network architecture to significantly optimize the performance of communications whose information can be determined at compile time (static communications). For static communications, *constant propagation* supports the compiled communication optimization approach. The analysis of NPB communication characteristics indicates that compiled communication can be applied to a large portion of the communications in the benchmarks. In particular, the majority of collective communications are static. We conclude that the compiled communication technique is worth proceeding.

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COLLEGE OF ARTS & SCIENCES

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To Mom, Dad, Brothers & Sisters, Mona, Azim, Nouri, the Issas, and the Carters. . .

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ABSTRACT

In this research, we investigate the communication characteristics of the Message Passing Interface (MPI) implementation of the NAS parallel benchmarks and study the feasibility and effectiveness of *compiled communication* on MPI programs. Compiled communication is a technique that utilizes the compiler knowledge of both the application communication requirement and the underlying network architecture to significantly optimize the performance of communications whose information can be determined at compile time (static communications). For static communications, *constant propagation* supports the compiled communication optimization approach. The analysis of NPB communication characteristics indicates that compiled communication can be applied to a large portion of the communications in the benchmarks. In particular, the majority of collective communications are static. We conclude that the compiled communication technique is worth proceeding.

CHAPTER 1

INTRODUCTION

As microprocessors become more and more powerful, clusters of workstations have become one of the most common high performance computing environments. The standardization of the Message Passing Interface (MPI) [3] facilitates the development of scientific applications for clusters of workstations using explicit message passing as the programming paradigm and has resulted in a large number of applications being developed using MPI. Designing an efficient cluster of workstations requires the MPI library to be optimized for the underlying network architecture and the application workload.

Compiled communication has recently been proposed to improve the performance of MPI routines for clusters of workstations[15]. In compiled communication, the compiler determines the communication requirements in a program and statically manages network resources, such as multicast groups and buffer memory, using the knowledge of both the underlying network architecture and the application communication requirements. Compiled communication offers many advantages over the traditional communication method. However, this technique cannot be applied to communications whose information is unavailable at compile time. In other words, the way programmers use the MPI routines can greatly influence the effectiveness of the compiled communication technique.

While the existing study [8] shows that the majority of communications in scientific programs are static, that is, the communication information can be determined at compile time, the communication characteristics of MPI programs have not been investigated in this manner. Given the popularity of MPI, it is important to study the communications in MPI programs and establish the feasibility and effectiveness of compiled communication on such programs. This is the major contribution of this thesis. We use the NAS parallel benchmarks (NPB) [6], the popular MPI benchmarks that are widely used in industry and academia to evaluate high performance computing systems, as a case study in an attempt to determine potential benefits of applying the compiled communication technique to MPI programs.

We consider constant propagation when obtaining information for compiled communication. According to that information, we classify communications into three types: static communications, dynamic communications, and dynamically analyzable communications. We apply the classification to both point-to-point communications and collective communications. Static communications are communications whose information can be determined at compile time. Dynamically analyzable communications are communications whose information can be determined at runtime without incurring excessive overheads. Dynamic communications are communications whose information can be determined only at runtime. The compiled communication technique is most effective in optimizing static communications. It can be applied to optimize dynamically analyzable communications at runtime with some overheads. Compiled communication is least effective in handling dynamic communication, and usually one has to resort to traditional communication schemes. Our study shows that while the MPI programs involve significantly more dynamic communications in comparison to the programs studied in [8], static and dynamically analyzable communications still account for a large portion of all communications. In particular, the majority of collective communications are static. We conclude that compiled communication can be feasible and effective for MPI programs.

The rest of the thesis is organized as follows. Chapter 2 presents the related work. Chapter 3 gives a brief introduction of compiled communication and related approaches. Chapter 4 summarizes the NAS parallel benchmarks. Chapter 5 describes the methodology we used in this study. Chapter 6 presents the results of the study. Chapter 7 concludes the thesis.

CHAPTER 2

RELATED WORK

The characterization of applications is essential for developing an efficient distributed system, and its importance is evident by the large amount of existing work [6, 7, 8, 12]. In [6], the overall performance of a large number of parallel architectures was evaluated using the NAS parallel benchmarks. In [7], the NAS benchmarks were used to evaluate two communication libraries on the IBM SP machine. In [12], detailed communication workload resulted from the NAS benchmarks was examined. These evaluations all assume that the underlying communication systems are traditional communication systems and do not classify communications based on whether the communications are static or dynamic. The most closely related work to this research was presented in [8], where the communications in parallel scientific programs were classified as static and dynamic. It was found that a large portion of communications in parallel programs, which include both message passing programs and shared memory programs, are static and less than 1% of the communications are dynamic. Since then, both parallel applications and parallel architectures evolved, and more importantly, MPI has been standardized, resulting in a large number of MPI based parallel programs. In this work, we focus on MPI programs whose communications have not been characterized or classified as static nor dynamic.

CHAPTER 3

COMPILED COMMUNICATION

In this chapter, we will discuss the communication optimization techniques including those used in Fortran D [10] and PARADIGM [9] at the compiler level, MPI-FM [1] and U-Net [2] at the library level, and compiled communication. We will then show examples of compiled communication. Finally, we will examine the compilation issues involved in the compiled communication technique.

3.1 Communication Optimization Techniques

Optimizing communication performance is essential to achieve high performance computing. At the compiler level, communication optimization techniques usually attempt to reduce the number or the volume of the communications involved. In a completely different manner, communication optimization approaches at the library level try to optimize the messaging layers and achieve low latency for each communication by eliminating software overheads.

Fortran D, developed at Rice University, allows programmers to annotate a program with data distribution information and automatically generates message passing code for distributed memory machines. Fortran D uses data dependence analysis to perform a number of communication optimizations. The most important communication optimizations in this compiler include message vectorization, redundant message elimination, and message aggregation. Message vectorization combines many small messages inside a loop into a large one and places the message outside the loop in order to avoid the overhead of communicating the messages individually. Redundant message elimination avoids sending a message wherever possible if the content of the message is subsumed by previous communication. Message aggregation involves aggregating multiple messages that need to be communicated between the same sender and receiver. Most of such communication optimizations are performed within loop nests.

Another related research effort in the same field as Fortran D, at the compiler level, is the parallelizing compiler for distributed memory general purpose multicomputers (PARADIGM), developed at the University of Illinois at Urbana-Champaign. The optimization techniques introduced in Fortran D such as message vectorization, redundant message elimination, and message aggregation are performed in PARADIGM too. One difference in PARADIGM is that it uses data-flow analysis to obtain information, which exploits more optimization opportunities than the Fortran D compiler. PARADIGM also developed new communication optimization techniques such as coarse grain pipelining, which is used in loops where there are cross iteration dependences. If we assume that each processor must wait before it accesses any data due to data dependence across iterations, then the execution becomes sequential. Instead of serializing the whole loop, coarse grain pipelining overlaps parts of the loop execution, synchronizing to ensure the data dependences are enforced [9]. In addition, optimization techniques for irregular communications are also developed in PARADIGM.

In general, the communication optimizations in the compiler approaches try to reduce the number or the volume of communications using either data-dependence analysis or data-flow analysis. They assume a simple communication interface such as the standard library, which hides the hardware details from the users. Thus, architecture dependent optimizations are usually not done in the compiler. Next, we will look at communication optimizations at the library level, which usually contain architecture dependent optimizations. Let us first introduce some background about library based optimizations. Researchers have developed libraries that provide means of executing parallel code on Ethernet-connected clusters of workstations instead of the highly parallel machines that are connected via dedicated hardware. The major challenge in clusters of workstations is efficient communication. The current most common messaging layer used for clusters of workstations is TCP/IP, which only delivers a portion of the underlying communication hardware performance to the application level due to large software overhead.

In an attempt to reduce software overhead, Chien and Lauria [1] designed the Fast Messages (FM) library. The Fast Messages library optimizes the software messaging layer between the lower level communication services and the network's hardware. The basic feature here is to provide a reliable in-order delivery of messages, which itself involves solutions for many critical messaging layer issues such as flow control, buffer management, and division of labor between the host processor and the network co-processor. This messaging layer, FM, uses a high performance optimistic flow control called return-to-sender, which is based on the assumption that the receiver polls the network in a timely manner, removing packets before its receive queue gets filled [1]. The library assumes simple buffer management in order to minimize software overhead in the network co-processor, making the co-processor free to service the fast network. Assigning as much functionality as possible to the host processor also frees the co-processor to service the network and achieves high performance. MPI-FM [1] is a high performance implementation of MPI for clusters of workstations built on top of the Fast Messages library to achieve low latency and high bandwidth communication.

In another attempt to achieve low latency and high bandwidth communication in a network of workstations, the user-level network (U-Net) moves parts of the communication protocol processing from the kernel level to the user level. In their study, Basu [2] argues that the whole protocol should be placed in the user level, and that the operating system task should be limited to basically ensure the protection of direct user-level accesses to the network. The goal here is to remove the operating system completely from the critical path and to provide each process the illusion of owning the network interface to enable the user-level accesses to high-speed communication devices. Using U-Net, the context switching when accessing the network devices, which incurs large overheads, is eliminated.

Communication optimizations at the library level can be architecture or operating system dependent. Such optimizations will benefit both traditional and compiled communication models. However, since a communication library does not have the information about the sequence of communications in an application, the optimization is inherently limited as it cannot be applied across communication patterns.

Compiled communication overcomes the limitations of the traditional compiler communication optimization approaches and the library based optimization schemes. During the compilation of an application, compiled communication gathers information about the application, and it uses such information together with its knowledge of the underlying network hardware to realize the communication requirements. As a result, *compiled communication can perform architecture or operating system dependent optimizations across communication patterns*, which is impossible in both the traditional compiler and the library based optimization approaches.

3.2 Examples of Compiled Communication

To illustrate the compiled communication technique, we will present two examples to show how compiled communication works. Figure 3.1 shows an MPI code segment of two MPI_Scatterv function calls. If we assume that IP-multicast is used to realize the MPI_Scatterv communication, then we need to create and destroy multicast groups before and after the movement of data. The non-user level library supporting



Figure 3.1. Traditional and Compiled Communication group management schemes the IP-multicast operation would replace each MPI_Scatterv call in the figure with calls to three other library routines in the following order:

- MPI_Open_Group: opens a group for a set of nodes.
- MPI_Move_Data: corresponds to the data movement operation.
- MPI_Close_Group: closes a group for a set of nodes.

As shown in the lower left hand-side of Figure 3.1, under the traditional scheme, two calls to MPI_Open_Group and two calls to MPI_Close_Group for the two MPI_Scatterv calls must be made. The compiled communication technique can generate code shown in the right hand-side of Figure 3.1 if the compiler can decide that the communication patterns for the two MPI_Scatterv calls are the same. In this case, the group would stay opened or alive until the end of the second MPI_Scatterv call. As can be seen in the figure, compiled communication removes one MPI_Open_Group and one MPI_Close_Group operations. Notice that MPI_Open_Group and MPI_Close_Group operations are expensive as they involve collective communication. Another potential optimization that compiled communication may apply occurs if the two scatter calls are adjacent, meaning no code is in between. In this situation, it can aggregate the content of each scatter communication and perform a single communication or data movement.

The second example assumes the underlying network is an optical network, where communications are connection-oriented, that is a path must be established before data movement occurs. In this case, compiled communication technique can also be beneficial. Let us consider the same example in Figure 3.1. The traditional execution of the MPLScatterv communication in an optical network will involve requesting connections, performing the data movement operation, and releasing the connections. This means that for the two MPLScatterv calls, we will request and release the connections twice. In contrast, compiled communication technique will only request the connection one time for both MPLScatterv calls assuming the connections for the second MPLScatterv is known by the compiler to be the same as the first MPLScatterv call. Also, we only need to perform one connection release for the two MPLScatterv calls.

From the examples, we can see that the advantages of using compiled communication approach include the following. First, compiled communication can eliminate some runtime communication overhead such as groups management. Second, compiled communication can use *long-lived* connections for communications and amortize the startup cost over a number of messages. Third, compiled communication can improve network resource utilization by using off-line resource management algorithms. Last but not the least, compiled communication can optimize arbitrary communication patterns as long as the communication information can be determined at compile time.

The limitation of compiled communication is that it cannot apply to communications whose information cannot be determined at compile time. Thus, the effectiveness of compiled communication depends on whether the communication information can be obtained at compile time. As shown in the next subsection, different ways to use the communication routines can greatly affect the possibilities for the compiler to obtain sufficient information for the compiled communication technique. Thus, to determine the effectiveness of compiled communication on MPI applications, the communication characteristics in such applications must be investigated.

3.3 Compiler Analysis to Support Compiled Communication

In this section, we will discuss the compilation issues involved in the compiled communication approach. We start by some examples to show the challenges a compiler must deal with in such an approach; then, we discuss the *constant propagation*, which is one of the important techniques to obtain information for compiled communication. Another related technique called a demand driven constant propagation is worth mentioning while, for the purpose of this thesis, a standard constant propagation algorithm like the one we will present soon is enough.

3.3.1 Challenges in Compiler to Support Compiled Communication Technique

Different programmers have different styles of coding, which can greatly affect the possibility of obtaining sufficient information as well as the technique to collect such information to support compiled communication. Assume that compiled communication requires the information about the communication pattern, that is the source-destination relationship. Let us consider the examples in Figure 3.2 for a commonly used nearest neighbor communication. By only examining the MPI function calls, we cannot determine the type of the communications involved in the code segments. Depending on the context, the communication can be either static, dynamic, or dynamically analyzable.

In Figure 3.2 part (a), the classification of the MPLSend function calls are considered static since the information in regard to the communication patterns including values for *north*, east, south, and west can be determined using some compiler algorithm. In other words, the relation between the sender (my_rank) and the receivers $(my_rank + north, east, south, or west)$ can be determined statically, and the communication pattern for each MPLSend routine can be decided. In this case, one communication optimization that compiled communication would consider is the transformation of the point to point send calls into a collective scatter operation. On the other hand, if the MPLSend routines are used in the context as shown in part (b) of Figure 3.2, then the compiler will mark the MPLSend function calls to be dynamic since different invocations of the nearest_neighbor routine with different parameters may result in different communication patterns. The communication patterns cannot be determined at compile time. Also note that aliasing is a problem that would prevent the compiled communication technique from determining the classification of a communication. Part (c) assumes that the communication patterns involve array elements, *dest*. This corresponds to the dynamically analyzable communication classification that we discussed earlier. The compiler realizes that the array is being used many times in the MPLSend function calls. Thus, the compiler decides to pay a little overhead at runtime to determine the array elements' values, and thus the communication patterns of the four MPI_Send routines, so that some optimizations can be applied at runtime. Notice that the runtime overhead is amortized over multiple communications.

3.3.2 An Example of Compiler Analysis to Support Compiled Communication

Depending on the type of communication, point-to-point or collective, the compiler must determine specific information in order to support compiled communication. For point-to-point communication, the compiler must decide the communication pattern, that is the source-destination relationship. When handling collective communication, the compiler must determine all the nodes involved in



Figure 3.2. Compiler challenges to support Compiled Communication example



Non-Constants

Figure 3.3. The lattice for constant propagation for a single program variable the communication, and sometimes it also needs to determine the initiator of the communication.

To obtain such information, the compiler usually needs to decide a value of a variable, and whether a variable and/or a data structure is modified in a code segment. We will consider a constant propagation algorithm that uses data-flow analysis in order to satisfy certain conditions for performing any applicable optimizations. Note that this algorithm is a modified version of a general constant propagation algorithm presented in [5]. A program that consists of a set of procedures is represented by a flow graph (FG). $G_{proc} = \{N_{proc}, E_{proc}\}$ represents a directed control flow graph of procedure proc. Each node in N_{proc} represents a statement in procedure proc, and each edge in E_{proc} represents transfer of control among the statements. Data-flow information can be gathered by setting up and solving systems of data-flow equations that relate information at different points in the program. Figure 3.3 defines the lattice for constant propagation where the variable may take one of two kinds of values: non-constant (NC), or constant, {C₁, C₂,...}. Assuming a program that contains n variables, we use a vector $[v_1 = a_1, v_2 = a_2, ..., v_n = a_n], 1 \le i \le n$, to represent the data-flow information. A variable v_i has a value a_i , which can be either a non-constant (NC), or any constant, $\{C_1, C_2,...\}$. Every statement has local functions Gen and Kill that operate on statements of the forms S_1, S_2 , or S_3 , which are described below. These functions take a vector of data-flow information as input and produce an output vector. Gen(S) specifies the set of definitions in a statement S while Kill(S) specifies the set of definitions that are killed by a statement S. The following is a formal description of Gen and Kill.

Gen(S):

 $\underline{S_1: v_k = b}, \text{ where } b \text{ is a constant.}$ Input vector: $[v_1=a_1, v_2=a_2, ..., v_k=a_k, ..., v_n=a_n]$ Output vector: $[v_1=a_1, v_2=a_2, ..., v_k=b, ..., v_n=a_n]$

 $\frac{S_2: read(v_k)}{Input vector: [v_1=a_1 v_2=a_2,..., v_k=a_k,..., v_n=a_n]}$ Output vector: [v_1=a_1, v_2=a_2,..., v_k=NC,..., v_n=a_n]

 $\frac{S_3: v_k = v_i + v_j}{\text{Input vector: } [v_1 = a_1, ..., v_k = a_k, v_i = a_i, v_j = a_j, ..., v_n = a_n]}$ $Output vector: [v_1 = a_1, ..., v_k = b, v_i = a_i, v_j = a_j, ..., v_n = a_n]$ $b = a_i + a_j \quad \text{if } (a_i \text{ and } a_j \text{ are constants})$ $b = \text{NC} \qquad \text{if } (a_i \text{ or } a_j \text{ is non-constant})$

Kill(S):

$$\frac{S_{1}: v_{k} = b}{\text{Input vector: } [v_{1}=a_{1}, v_{2}=a_{2},..., v_{k}=a_{k},..., v_{n}=a_{n}]}$$

Output vector: $[v_{1}=a_{1}, v_{2}=a_{2},..., v_{k}=\text{NC},..., v_{n}=a_{n}]$

 $\frac{S_2: read(v_k)}{Input vector: [v_1=a_1 v_2=a_2,..., v_k=a_k,..., v_n=a_n]}$ Output vector: [v_1=a_1, v_2=a_2,..., v_k=NC,..., v_n=a_n]

 $\frac{S_{3}: v_{k} = v_{i} + v_{j}}{\text{Input vector: } [v_{1}=a_{1},..., v_{k}=a_{k}, v_{i}=a_{i}, v_{j}=a_{j},..., v_{n}=a_{n}]}$ $\text{Output vector: } [v_{1}=a_{1},..., v_{k}=\text{NC}, v_{i}=a_{i}, v_{j}=a_{j},..., v_{n}=a_{n}]$

Note that the "+" is a typical binary operator we use as an example. Other binary operators can be handled in a similar manner. We also define the following functions over the data-flow information vectors.

Union: a function that returns a vector representing the union of two data-flow information vectors.

Input vectors:
$$[v_1=a_1, v_2=a_2, ..., v_n=a_n]$$
 and $[v_1=b_1, v_2=b_2, ..., v_n=b_n]$.
Output vector: $[v_1=z_1, v_2=z_2, ..., v_n=z_n]$ for each i, $1 \le i \le n$,
 $z_i = a_i$ if $(a_i \text{ is } C \text{ and } b_i \text{ is } NC)$
 $z_i = b_i$ if $(b_i \text{ is } C \text{ and } a_i \text{ is } NC)$
 $z_i = a_i$ if $(a_i=b_i \text{ and } a_i \text{ is } C)$
 $z_i = NC$ if $(a_i \text{ and } b_i \text{ are both } NC)$

Join: a function that returns a vector representing the join of two data-flow information vectors.

Input vectors: $[v_1=a_1, v_2=a_2, ..., v_n=a_n]$ and $[v_1=b_1, v_2=b_2, ..., v_n=b_n]$. Output vector: $[v_1=z_1, v_2=z_2, ..., v_n=z_n]$ for each i, $1 \le i \le n$, $z_i = a_i$ if $(a_i = b_i \text{ and } a_i \text{ is C})$ $z_i = \text{NC}$ if $(a_i = b_i \text{ and } a_i \text{ is NC})$ $z_i = \text{NC}$ if $(a_i \ne b_i)$ In: a vector that reaches the beginning of a statement S, taking into account the flow of control throughout the whole program, which includes statements in blocks outside of S or within which S is nested.

 $In[S] = Join(Out[S_{pred}])$ where *pred* is the set of all predecessors of statement S. Out: a vector that reaches the end of a statement S, again taking into account the control flow throughout the entire program.

Out[S] = Union(Gen(In[S]), Kill(In[S])).

Now that we have established the data-flow equations, we can present an algorithm for constant propagation. Given an input of a control flow graph for which the Gen[B] and Kill[B] have been computed for each statement S, we compute In[S]and Out[S] for each statement S. The following is an iterative algorithm for constant propagation.

- 1. for each statement S do $Out[S] := [V_1=NC, V_2=NC, ..., V_n=NC];$
- 2. for each statement S do
- 3. $In[S] := Join(Out[S_{pred}]); /* Ignoring predecessors with back-edges */$
- 4. $\operatorname{Out}[S] := \operatorname{Union}(\operatorname{Gen}(\operatorname{In}[S]), \operatorname{Kill}(\operatorname{In}[S]));$
- 5. end
- 6. change := true;
- 7. while change do
- 8. change := false;
- 9. for each statement S do
- 10. $\operatorname{In}[S] := \operatorname{Join}(\operatorname{Out}[S_{pred}]);$
- 11. oldout := Out[S];
- 12. $\operatorname{Out}[S] := \operatorname{Union}(\operatorname{Gen}(\operatorname{In}[S]), \operatorname{Kill}(\operatorname{In}[S]));$
- 13. if $Out[S] \neq oldout$ then *change* := true;
- 14. end
- 15. end

For each statement S, we initialize the elements of vector Out[S] to be NC. Then, we calculate the data-flow vectors In and Out for each statement while ignoring predecessors with back-edges, which allows constants outside a loop to be propagated into the loop. This step or pass emulates the straight line execution of the program. Following that step, we iterate until the Out/In vectors for all nodes are fixed. In order to iterate until the In's and Out's converge, the algorithm uses a Boolean *change* to record on each pass through the statements whether any In has changed.

Table 3.1 shows the effect of executing lines 2-5 of the algorithm on the control flow graph example in Figure 3.4. We consider the following evaluation order: S1, S2, S3, S4, S6, S7, S8, S10, S9, S5.

Stmnt	Function	x	У	\mathbf{Z}	k	i
S_1	In	NC	NC	NC	NC	NC
	Out	1	NC	NC	NC	NC
S_2	In	1	NC	NC	NC	NC
	Out	1	1	NC	NC	NC
S_3	In	1	1	NC	NC	NC
	Out	1	1	NC	NC	0
S_4	In	1	1	NC	NC	0
	Out	1	1	NC	NC	0
S_5	In	1	1	NC	3	0
	Out	1	1	NC	3	1
S_6	In	1	1	NC	NC	0
	Out	1	1	NC	NC	0
S_7	In	1	1	NC	NC	0
	Out	1	1	2	NC	0
S_8	In	1	1	2	NC	0
	Out	1	1	2	2	0
S_9	In	1	1	NC	NC	0
	Out	1	1	NC	3	0
S_{10}	In	1	1	NC	NC	0
	Out	1	1	3	NC	0

Table 3.1. Effect of executing constant propagation algorithm (lines 2-5) on the sample control flow graph

At this point, we look at statement S_9 , the last statement before incrementing *i*, and find that *z* is a non-constant due to the join of statements S_8 (z=2) and S_{10} (z=3)



Figure 3.4. Sample control flow graph for illustrating constant propagation

while x, y, k, and i have constant values, yet such variables may have non-constant values upon the termination of the algorithm.

We next execute lines (7-15) of the algorithm, which is the iterative part that computes the final In and Out vectors of each statement S for the sample control flow graph. Table 3.2 shows the results. If we look at statement S_4 , we notice that *i* is now a non-constant since each incoming edge gives different constant values of *i*. At S_5 , *z* is a non-constant, as determined in lines 2-5 of the algorithm, and its value gets propagated to any outgoing edge, which is S_4 in this case. Also, *k* is set to be a non-constant at S_4 since the predecessor statements (S_3 and S_5) give two different values of *k*.

Stmnt	Function	x	У	\mathbf{Z}	k	i
S_1	In	NC	NC	NC	NC	NC
	Out	1	NC	NC	NC	NC
S_2	In	1	NC	NC	NC	NC
	Out	1	1	NC	NC	NC
S_3	In	1	1	NC	NC	NC
	Out	1	1	NC	NC	0
S_4	In	1	1	NC	NC	NC
	Out	1	1	NC	NC	NC
S_5	In	1	1	NC	3	NC
	Out	1	1	NC	3	NC
S_6	In	1	1	NC	NC	NC
	Out	1	1	NC	NC	NC
S_7	In	1	1	NC	NC	NC
	Out	1	1	2	NC	NC
S_8	In	1	1	2	NC	NC
	Out	1	1	2	2	NC
S_9	In	1	1	NC	NC	NC
	Out	1	1	NC	3	NC
S_{10}	In	1	1	NC	NC	NC
	Out	1	1	3	NC	NC

Table 3.2. Effect of executing constant propagation algorithm (lines 7-15) on the sample control flow graph

Since some of the "Out" vectors changed in the first iteration of the *while* loop, the boolean *change* was reset to *true* causing another iteration, which does not introduce any new changes in any of the Out vectors for this particular control flow graph example. Thus, the algorithm terminates.

In brief, we have shown that the analysis of compiled communication is not trivial, yet feasible. The use of an iterative algorithm for constant propagation, as one of many techniques a compiler applies to gather information, is essential to make compiled communication effective when applying possible optimization, and we have the intention to implement it in a later phase of our pursuit of compiled communication.

CHAPTER 4

NAS PARALLEL BENCHMARKS

The NAS parallel benchmarks (NPB) [6] were developed at the NASA Ames research center to evaluate the performance of parallel and distributed systems. The benchmarks, which are derived from computational fluid dynamics (CFD), consist of five parallel kernels (EP, MG, CG, FT, and IS) and three simulated applications (LU, BT, and SP). In this work, we study NPB 2.3 [11], the MPI-based implementation written and distributed by NAS. NPB 2.3 is intended to be run, with little or no tuning, to approximate the performance a typical user can expect to obtain for a portable parallel program. The following is a brief overview of each of the benchmarks, and a detailed description can be found in [11, 16].

- Parallel kernels
 - The Embarrassingly Parallel (EP) benchmark generates pairs of (N = 2 ^ M) Gaussian random deviates according to a specific scheme and tabulates the pairs. The benchmark is used in many Monte Carlo simulation applications. The benchmark requires very few inter-processor communications.
 - The Multigrid (MG) benchmark solves four iterations of a V-cycle multigrid algorithm to obtain an approximate solution u to the discrete Poisson problem $\Delta^2 u = v$ on a 256 × 256 × 256 grid with periodic boundary conditions. This benchmark contains both short and long distance regular communications.

- The Conjugate Gradient(CG) benchmark uses the inverse power method to find an estimate of the smallest eigenvalue of a symmetric positive definite sparse matrix (N x N) with a random pattern of non-zeroes. This benchmark contains irregular communications.
- The Fast Fourier Transform (FT) benchmark solves a partial differential equation (PDE) using forward and inverse FFTs. 3D FFTs (N x N x N grid size) are a key part of a number of computational fluid dynamics (CFD) applications and require considerable communications for operations such as array transposition.
- The Integer Sort (IS) benchmark sorts N keys in parallel. This kind of operation is important in *particle method* codes.
- Simulated parallel applications
 - The LU decomposition (LU) benchmark solves a finite difference discretization of the 3-D compressible Navier-Stokes equations through a block-lower-triangular block-upper-triangular approximate factorization of the original difference scheme. The LU factored form is cast as a relaxation, and is solved by the symmetric successive over-relaxation (SSOR) numerical scheme. The grid size is (N x N x N).
 - The Scalar Pentadiagonal (SP) benchmark solves (N x N x N) multiple independent systems of non-diagonally dominant, scalar pentadioganal equations.
 - The block tridiagonal (BT) benchmark solves (N x N x N) multiple, independent systems of non-diagonally dominant, block tridioganal equations with a (5x5) block size. SP and BT are similar in many respects; however, the communication to computation ratio of these two benchmarks is very different.

Benchmark	# of lines	# of MPI routines
EP	346	10
MG	2540	41
CG	1841	40
FT	2193	20
IS	1097	21
LU	5194	53
SP	4892	48
BT	5632	54

 Table 4.1.
 Summary of the NAS benchmarks

Table 4.1 summarizes the basic information about the benchmark programs. The second column shows the code size, and the third column shows the number of all MPI routines used in the program, including non-communication MPI routines such as *MPI_Init*. As can be seen in the table, each of the benchmarks makes a fair number of MPI calls. The MPI communication routines used in the benchmarks are *MPI_Alltoall*, *MPI_Alltoallv*, *MPI_Allreduce*, *MPI_Barrier*, *MPI_Bcast*, *MPI_Send*, *MPI_Isend*, *MPI_Recv*, and *MPI_Irecv*. In the next chapter, we will describe the parameters and the functionality of these routines. Details about MPI can be found in [3].

CHAPTER 5

METHODOLOGY

In this chapter, we describe the methodology we used. We will present the assumptions, the methods to classify communications, and the techniques to collect statistical data. From now on, we will use the words "program" and "benchmark" interchangeably.

5.1 Types of communications

The communication information needed by compiled communication depends on the optimizations to be performed. In this study, we assume that the communication information needed is the *communication pattern*, which specifies the source-destination pairs in a communication. Many optimizations can be performed using this information. In a circuit-switched network, for example, compiled communication can use the knowledge of communication patterns to pre-establish connections and eliminate runtime path establishment overheads. When multicast communication is used to realize collective communications, compiled communication can use the knowledge of communications to perform group management statically.

We classify the communications into three types: static communications, dynamic communications, and dynamically analyzable communications. The classification applies to both collective communications and point-to-point communications. A static communication is a communication whose pattern information is determined at compile time via constants. A dynamic communication is a communication whose pattern information can only be determined at runtime. A dynamically analyzable communication is a communication whose pattern information can be determined at runtime without incurring excessive overheads. In general, dynamically analyzable communications usually result from communication routines that are invoked repeatedly with one or more symbolic constant parameters. Since the symbolic constants can be determined once at runtime (thus, without incurring excessive overheads) and be used many times in the communications, we distinguish such communications from other dynamic communications. The parameterized communications in [8], that is, communications whose patterns can be represented at compile time using some symbolic constant parameters, belong to the dynamically analyzable communications in our classification. Note that some techniques have been developed to deal with parametrized communications, and we may incorporate such techniques with our compiled communication approach to optimize dynamically analyzable communication. We plan on such integration in the future.

5.2 Assumptions about the compiler

The compiler analysis technique greatly affects the compiler's ability to identify static communications. In the study, we emulate the compiler and analyze the programs by hand to mark the communication routines. We make the following assumptions:

- The compiler does not support array analysis. All array elements are considered unknown variables at compile time. We treat an array as a scalar and assume an update of a single array element modifies the whole array.
- The compiler has perfect scalar analysis: it can always determine the value of a scalar if the value can be determined.

• The compiler does not have inter-procedural analysis. Information cannot be propagated across procedure boundaries. The parameters of a procedure are assumed to be unknown. We also assume that simple in-lining is performed: procedures that are called only in one place in the program are in-lined.

5.3 Classifying communications

The communication routines in the NAS benchmarks include five collective communication routines: MPI_Allreduce, MPI_Alltoall, MPI_Alltoallv, MPI_Barrier, and MPI_Bcast, and four point-to-point communication routines: MPI_Send, MPI_Isend, MPI_Irecv, and MPI_Recv. Each collective communication routine represents a communication while a point-to-point communication is represented by a pair of MPI_Send/MPI_Isend and MPI_Recv/MPI_Irecv routines. We assume that the benchmarks are correct MPI programs. Thus, MPI_Send/MPI_Isend routines are matched with MPI_Recv/MPI_Irecv routines, and the information about point-to-point communications is derived from MPI_Send and MPI_Isend routines.

All MPI communication routines have a parameter called *communicator*, which contains the information about the set of processes involved in the communication. To determine the communication pattern information for each communication, we must determine the processes in the corresponding communicator. Next, we will describe how we deal with the communicator and how we mark each MPI communication routine.

Communicator

The communicators used in the NAS benchmarks are either the MPI builtin communicator, *MPI_COMM_WORLD*, which specifies all processes for a task, or derived from *MPI_COMM_WORLD* using *MPI_Comm_split* and/or *MPI_Comm_dup* functions. We assume that *MPI_COMM_WORLD* is known to the compiler. This is equivalent to assuming that the program is compiled for a particular number of nodes for execution. A dynamically created communicator is static if we can determine the ranks of all the nodes in the communicator with respect to *MPI_COMM_WORLD* at compile time. If a communicator is a global variable and is used in multiple communications, it is considered as a dynamically analyzable communicator. The rationale to treat such a communicator as a dynamically analyzable communicator is that a communicator typically lasts for a long time in the execution and is usually used in many communications. The overhead to determine the communicator information at runtime is small when amortized over the number of communications that use the communicator. A communicator is considered dynamic if it is neither static nor dynamically analyzable.

For a communication to be static, the corresponding communicator must be static. For a communication to be dynamically analyzable, the communicator can be either static or dynamically analyzable.

MPI_Barrier

The prototype for this routine is *int* $MPI_Barrier(MPI_Comm\ comm)$. The communication resulted from this routine is implementation dependent. However, once the compiler determines the communicator comm, it also determines the communication pattern for a particular MPI implementation. Thus, the communication is static if comm is static, dynamically analyzable if comm is dynamically analyzable, and dynamic if comm is dynamic. Here is a FORTRAN example code segment from the CG benchmark:

mpi_barrier(MPI_COMM_WORLD, ierr)

As we have established above, *MPI_COMM_WORLD* is assumed to be known by the compiler, and so this routine call is considered static.

MPI_Alltoall

The prototype for this routine is int MPI_Alltoall(void* sendbuf,int sendcount, MPI_Datatype sendtype, void* recvbuf, int recvcount, MPI_Datatype recvtype, MPI_Comm comm). This routine results in all nodes in comm sending messages to all other nodes in comm. Thus, once comm is determined, the communication pattern for MPI_Alltoall can be decided. The communication is static if comm is static, dynamically analyzable if comm is dynamically analyzable, and dynamic if comm is dynamic. The following is an example FORTRAN code segment of a dynamically analyzable MPI_Alltoall routine from the FT benchmark:

mpi_alltoall(xin, ntotal/(np*np), dc_type, xout, ntotal/(np*np), dc_type, commslice1, ierr)

The *commulice*1 communicator parameter is dynamically analyzable since it is a result of an *MPI_COMM_WORLD split* operation that in fact involves another parameter being read from a file at runtime. With a little overhead, the communicator information can be determined at runtime.

MPI_Alltoallv

The prototype for this routine is int MPLAlltoallv(void* sendbuf, int *sendcounts, int *sdispls, MPLDatatype sendtype, void* recvbuf, int *recvcounts, int *rdispls, MPLDatatype recvtype, MPLComm comm). The communication pattern for this routine depends on the values of the sendcount array elements. Since we assume that the compiler does not have array analysis in this study, all <math>MPLAlltoallv routines are marked as dynamic. The next C code segment, taken from the IS benchmark, shows an example of such routines.

MPI_Alltoallv(key_buff1,send_count, send_displ, MPI_INT, key_buff2, recv_count, recv_displ, MPI_INT, MPI_COMM_WORLD)

MPI_Allreduce

The prototype for this routine is int $MPI_Allreduce(void* sendbuf, void* recvbuf, int count, MPI_Datatype datatype, MPI_Op op, MPI_Comm comm)$. The communication pattern in this routine is implementation dependent. It is roughly equivalent to a reduction and a broadcast. Once the communicator comm is determined, the communication pattern for a particular implementation can be decided. Thus, the communication is static if comm is static, dynamically analyzable if comm is dynamic if comm is dynamic. Here is a FORTRAN example code segment from EP:

mpi_allreduce(sx, x, 1, dp_type, MPI_SUM, MPI_COMM_WORLD, ierr)

This is a static routine since we have a static communicator.

MPI_Bcast

The prototype for this routine is int MPI_Bcast(void* buffer, int count,

 $MPI_Datatype\ datatype,\ int\ root,\ MPI_Comm\ comm)$. The communication pattern of this routine is root sending a message to all other nodes in the communicator comm. Thus, if either comm or root is dynamic, the communication is dynamic. If both comm and root can be determined at compile time, the communication is static. Otherwise, the communication is dynamically analyzable. The following FORTRAN example code segment from the MG benchmark shows that the MPI_Bcast is static since the communicator mpi_comm_world and root(0) are known statically:

mpi_bcast(lt, 1, MPI_INTEGER, 0, mpi_comm_world, ierr)

MPI_Send

The prototype for this routine is *int MPI_Send(void* buf, int count, MPI_Datatype datatype, int dest, int tag, MPI_Comm comm)*. The analysis of this routine is somewhat tricky: the instantiation of the routine at runtime results in different source-destination pairs for different nodes. For an *MPI_Send* to be static, all the source-destination pairs resulted from the routine must be determined at compile time. This requires the followings:

- The communicator, *comm*, should be static.
- The relation between ranks of the destination and the source nodes should be static.
- If there are guard statements (if statement) protecting the routine, the effects of the guard statements should be static.

If any of the above is dynamic or dynamically analyzable, the communication is marked as dynamic or dynamically analyzable. We show three different examples corresponding to the above analysis. The following is a C code segment from the ISbenchmark:

if(my_rank < comm_size - 1) MPI_Send(key_array[total_local_keys-1], 1, MPI_INT, my_rank + 1, 1000, MPI_COMM_WORLD)

the source, my_rank , and $comm_size$ as well as MPI_COMM_WORLD are static variables. Thus, the effect of the *if* statement is static. The relation between ranks of the destination and the source nodes is static, destination is my_rank+1 . Finally, the communicator, MPI_COMM_WORLD , is static. As a result, this routine is considered static. If we assume MPI_COMM_WORLD contains 4 nodes, then the static communication pattern resulting from this routine is $\{0 \rightarrow 1, 1 \rightarrow 2, 2 \rightarrow 3\}$. Here, we use the notion $x \rightarrow y$ to represent node x sending messages to node y. On the other hand, the following *FORTRAN* code segment taken from the *LU* benchmark shows an example of a dynamic *MPI_Send* routine:

mpi_send(dum(1,jst), 5*(jend-jst+1), dp_type, south, from_n, mpi_comm_world, status, ierror)

The destination and the source relationship here is dynamic due to the fact that the destination *south* is a variable that changes during the program execution. The next FORTRAN code segment, from the SP benchmark, shows an example of a dynamically analyzable MPI_Isend routine:

The communicator *comm_solve* is dynamically analyzable as it was a result of MPI communicator *split* and *dup* operations. The information in *comm_solve* can be obtained with a little runtime overhead. In addition, the relationship between the source and the destination is dynamically analyzable since *successor* is an array whose elements are initialized at the start of the program execution. The value of successor(1) can be determined at runtime without much overhead.

MPI_Isend

The analysis of this routine is similar to that of MPI_Send.

5.4 Data collection

To collect dynamic measurement of the communications, we instrument MPI operations by implementing an MPI wrapper that allows us to monitor the MPI communication activities at runtime. Notice that we cannot use built-in MPI monitoring utility provided by the existing MPI implementation since we must distinguish among static, dynamic, and dynamically analyzable communications. Such information is not presented in the original MPI routines. To obtain the information, we examine the source code and mark each of the MPI communication routines by hand. In the MPI wrapper, we record all MPI operations with their respective parameters (as well as a field indicating whether the communication is static, dynamic, or dynamically analyzable) in a local trace file. After the execution of the program, we analyze the trace files for all the nodes off-line to obtain the dynamic measurements. Most trace-based analysis systems use a similar approach [13].

CHAPTER 6

RESULTS & IMPLICATIONS

program	communication routines					
EP	Static: 4 MPI_Allreduce, 1 MPI_Barrier					
CG	Static: 1 MPI_Barrier					
	Dynamic: 10 MPI_Send					
MG	Static: 6 MPI_Allreduce, 9 MPI_Barrier					
	6 MPI_Bcast					
	Dynamic: 12 MPI_Send					
FT	Static: 2 MPI_Barrier, 2 MPI_Bcast					
	Dynamically analyzable: 3 MPI_Alltoall					
IS	Static: 1 MPI_Allreduce, 1 MPI_Alltoall					
	$1 MPI_Send$					
	Dynamic: 1 MPI_Alltoallv					
LU	Static: 6 MPI_Allreduce, 1 MPI_Barrier					
	9 MPI_Bcast					
	Dynamically Analyzable: 4 MPI_Send					
	Dynamic: 8 MPI_Send					
BT	Static: 2 MPI_Allreduce, 2 MPI_Barrier					
	$3 MPI_Bcast$					
	Dynamically Analyzable: 12 MPI_Isend					
SP	Static: 2 MPI_Allreduce, 2 MPI_Barrier					
	3 MPI_Bcast					
	Dynamically Analyzable: 12 MPI_Isend					

 Table 6.1. Static classification of MPI communication routines

Table 6.1 shows the static classification of the communication routines in each program. All but one collective communication routine $(MPL_alltoallv \text{ in } IS)$ in the benchmarks are either static or dynamically analyzable. In contrast, a relatively larger portion of point-to-point communication routines are dynamic. Figure 6.1 summarizes the static counts of different communications. Among the 126 communication routines in all the benchmarks, 50.8% are static, 24.6% are



Figure 6.1. Summary of static measurement

dynamically analyzable, and 24.6% are dynamic. This measurement shows that there are not many MPI communication routines in a program, and that using the demand driven method [14], which obtains program information on demand, to analyze the program and obtain information for compiled communication is likely to perform better than using the traditional exhaustive program analysis approach.

Next we will show the dynamic measurements of the communications. To reveal the impact of the problem sizes and the number of nodes in the system on the communications, we will present results for four cases: large problems ('A' class in the NPB-2.3 specification) on 16 nodes, small problems ('S' class in the NPB-2.3 specification) on 16 nodes, large problems on 4 nodes, and small problems on 4 nodes.

6.1 Results for large problems on 16 nodes

Table 6.2 shows the dynamic measurements of the number and the volume for the three types of communications in each of the benchmarks. The number of communications is the number of times a communication routine is invoked. For collective communications, the invocations of the corresponding routine at different nodes are counted as one communication. For point-to-point communications, each invocation of a routine at each node is counted as one communication. The volume of communications is the total number of bytes sent by the communications. For example, EP has 5 static communications, which transfer 12.5KB of data. Different

program	type	number	number $\%$	volume	volume $\%$
	Static	5	100.0%	12.5KB	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	0.0%	0.03KB	0.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	47104	100.0%	2.24 GB	100.0%
	Static	100	0.9%	126 KB	0.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11024	99.1%	384 MB	100.0%
	Static	3	27.3%	$0.99 \mathrm{KB}$	0.0%
FT	Dynamically analyzable	8	72.7%	$3.77 \mathrm{GB}$	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	37	77.1%	$1.37 \mathrm{MB}$	0.4%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	22.9%	346 MB	99.6%
	Static	18	0.0%	28.6KB	0.0%
LU	Dynamically analyzable	12096	1.6%	3.96 GB	75.7%
	Dynamic	744036	98.4%	1.27 GB	24.3%
	Static	7	0.0%	11.1KB	0.0%
BT	Dynamically analyzable	77280	100.0%	14.1GB	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	0.0%	11.1KB	0.0%
SP	Dynamically analyzable	154080	100.0%	23.7GB	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.2. Dynamic measurement for large problems (SIZE = A) on 16 nodes

benchmarks exhibit different communication characteristics: in terms of the volume of communications, among the eight benchmarks, CG, MG, and IS are dominated by dynamic communications; EP contains only static communications; FT, BT, and SP are dominated by dynamically analyzable communications. LU has 75.7% dynamically analyzable communications and 24.3% dynamic communications. In comparison to the results in [8], the NAS parallel benchmarks have significantly less static communications and much more dynamic communications. However, static and dynamically analyzable communications still account for a large portion of the communications, which indicates that compiled communication can be effective if it can be applied to the two types of communications. The results also show that in order for compiled communication to be effective, it must be able to optimize dynamically analyzable communications.

program	type	number	volume	volume $\%$
EP	collective	5	$12.5 \mathrm{KB}$	100.0%
	point-to-point	0	0	0.0%
CG	collective	1	0.03B	0.0%
	point-to-point	6720	2.24 GB	100.0%
MG	collective	100	126KB	0.0%
	point-to-point	11024	384 MB	100.0%
FT	collective	11	$3.77 \mathrm{GB}$	100.0%
	point-to-point	0	0	0.0%
IS	collective	33	348 MB	100.0%
	point-to-point	15	0.06 KB	0.0%
LU	collective	18	$28.6 \mathrm{KB}$	0.0%
	point-to-point	756132	$5.24 \mathrm{GB}$	100.0%
BT	collective	7	11.1KB	0.0%
	point-to-point	77280	14.1GB	100.0%
SP	collective	7	11.1KB	0.0%
	point-to-point	154080	23.7 GB	100.0%

Table 6.3. Dynamic measurement for collective and point-to-point communications with large problems (SIZE = A) on 16 nodes

Since collective communication and point-to-point communication are implemented in a different manner, we will consider collective communication and point-topoint communication separately. Table 6.3 shows the number and the volume of collective and point-to-point communications in the benchmarks. The communications in benchmarks EP, FT, and IS are dominated by collective communications while the communications in CG, MG, LU, BT, and SP are dominated by point-to-point communications.

Table 6.4 shows the classification of collective communications in the benchmarks. As can be seen in the table, the collective communications in six benchmarks, EP, CG, MG, LU, BT, and SP are all static. Most of the collective communications in FT are dynamically analyzable. Only the collective communications in IS are mostly dynamic. The results show that most of collective communications are either static

program	type	number	number $\%$	volume	volume $\%$
	Static	5	100.0%	12.5KB	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	100.0%	$0.03 \mathrm{KB}$	100.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	100	100.0%	126KB	100.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	3	27.3%	$0.99 \mathrm{KB}$	0.0%
FT	Dynamically analyzable	8	72.7%	$3.77 \mathrm{GB}$	100%
	Dynamic	0	0.0%	0	0.0%
	Static	22	66.7%	$1.37 \mathrm{MB}$	0.4%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	33.3%	346 MB	99.6%
	Static	18	100.0%	28.6KB	100.0%
LU	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	100.0%	11.1KB	100.0%
BT	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	100.0%	11.1KB	100.0%
SP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.4. Dynamic measurement of collective communications with large problems (SIZE = A) on 16 nodes

or dynamically analyzable. The implication is that the compiled communication technique should be applied to optimize the MPI collective communication routines.

Table 6.5 shows the classification of point-to-point communications. Since EP and FT do not have point-to-point communication, we exclude these two benchmarks from the table. In comparison to collective communication, more point-to-point communications are dynamic. CG and MG contain only dynamic point-to-point communications. BT and SP contain only dynamically analyzable point-to-point communications. None of the benchmarks has a significant number of static point-to-point communications. However, since a significant portion of point-to-point communications are dynamically analyzable, compiled communication

program	type	number	number $\%$	volume	volume $\%$
	Static	0	0.0%	0	0.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	47104	100.0%	2.24 GB	100.0%
	Static	0	0.0%	0	0.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11024	100.0%	384 MB	100.0%
	Static	15	100.0%	$0.06 \mathrm{KB}$	100.0%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	0	0.0%	0	0.0%
LU	Dynamically analyzable	12096	1.6%	3.96GB	75.7%
	Dynamic	744036	98.4%	1.27 GB	24.3%
	Static	0	0.0%	0	0.0%
BT	D. ana	77280	100.0%	14.1GB	100.0%
	Dynamic	0	0.0%	0	0.0%
SP	Static	0	0.0%	0	0.0%
	Dynamically analyzable	154080	100.0%	$23.7 \mathrm{GB}$	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.5. Dynamic measurement of point-to-point communications with large problems (SIZE = A) on 16 nodes

can be effective for point-to-point communications if it is effective for dynamically analyzable communications.

Message sizes can greatly affect the ways the communications are performed. Figure 6.2 shows the summary of the message size distribution for collective communications in all the benchmarks. The summary is obtained by first computing the message size distribution in terms of percentage for each range of message sizes in each of the benchmarks. We then give equal weights to all the benchmarks that have the particular communication and calculate the average message size distribution in terms of percentage. The benchmarks only have one dynamically analyzable and one dynamic collective communications, so there is not much distribution for these cases. For static collective communications, the message sizes are mostly small (< 1KB). This indicates that static collective communications with small message sizes are important cases for compiled communication.



Figure 6.2. Message size distribution for collective communications (SIZE = A) on 16 nodes

Figure 6.3 shows the summary of the message size distribution for point-to-point communications in all the benchmarks. The summary is obtained in a similar manner to that of the collective communications case. The static point-to-point communications have a small message size while dynamic and dynamically analyzable point-to-point communications generally have medium to large message sizes.



Figure 6.3. Message size distribution for point-to-point communications (SIZE = A) on 16 nodes

program	type	number	number $\%$	volume	volume $\%$
	Static	5	100.0%	12.5KB	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	0.0%	0.03KB	0.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	47104	100.0%	$225 \mathrm{MB}$	100.0%
	Static	100	1.5%	126KB	0.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	6704	98.5%	7.83MB	100.0%
	Static	3	27.3%	0.99KB	0.0%
FT	Dynamically analyzable	8	72.7%	118MB	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	37	77.1%	0.69MB	19.4%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	22.9%	$2.86 \mathrm{MB}$	80.6%
	Static	7	0.0%	11.1KB	0.0%
BT	Dynamically analyzable	23520	100.0%	0.21GB	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	0.0%	11.1KB	0.0%
SP	Dynamically analyzable	38880	100.0%	0.18GB	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.6. Dynamic measurement for small problems (SIZE = S) on 16 nodes

6.2 Results for small problems on 16 nodes

In this section, we will show the results for executing the benchmarks with a small problem size on 16 nodes. Since LU cannot be executed in this setting, we will exclude it from the results.

Table 6.6 shows the dynamic measurement of the number and the volume for the three types of communications in each of the benchmarks. The results are similar to those for large problems except that a small problem size results in a small communication volume. In terms of the volume of communications, among the eight benchmarks, CG, MG, and IS are dominated by dynamic communications; EPcontains only static communications; FT, BT, and SP are dominated by dynamically analyzable communications. Static and dynamically analyzable communications still account for a large portion of the communications.

program	type	number	volume	volume $\%$
EP	collective	5	12.5KB	100.0%
	point-to-point	0	0	0.0%
CG	collective	1	0.03B	0.0%
	point-to-point	47104	225 MB	100.0%
MG	collective	100	126KB	1.6%
	point-to-point	6704	7.83MB	98.4%
FT	collective	11	118MB	100.0%
	point-to-point	0	0	0.0%
IS	collective	33	$3.55 \mathrm{MB}$	100.0%
	point-to-point	15	0.06KB	0.0%
BT	collective	7	11.1KB	0.0%
	point-to-point	23520	209 MB	100.0%
\overline{SP}	collective	7	11.1KB	0.0%
	point-to-point	38880	178MB	100.0%

Table 6.7. Dynamic measurement for collective and point-to-point communications with small problems (SIZE = S) on 16 nodes

Table 6.7 shows the number and the volume of collective and point-to-point communications in the benchmarks. The communications in benchmarks EP, FT, and IS are dominated by collective communications while the communications in CG, MG, BT, and SP are dominated by point-to-point communications. A smaller problem size does not significantly change the overall ratio between collective communications and point-to-point communications in these benchmarks.

Table 6.8 shows the classification of collective communications in the benchmarks. The results agree with previous results for large problems. The collective communications in EP, CG, MG, BT, and SP are all static. Most of the collective communications in FT are dynamically analyzable. Only the collective communications in IS are mostly dynamic. A smaller problem size does not change the distribution of static, dynamic, and dynamically analyzable collective communications in these benchmarks significantly.

program	type	number	number $\%$	volume	volume $\%$
	Static	5	100.0%	12.5KB	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	100.0%	$0.03 \mathrm{KB}$	100.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	100	100.0%	126KB	100.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	3	27.3%	0.99KB	0.0%
FT	Dynamically analyzable	8	72.7%	118MB	100%
	Dynamic	0	0.0%	0	0.0%
	Static	22	66.7%	692 KB	19.5%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	33.3%	$2.86 \mathrm{MB}$	80.5%
	Static	7	100.0%	11.1KB	100.0%
BT	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	100.0%	11.1KB	100.0%
SP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.8. Dynamic measurement of collective communications with small problems (SIZE = S) on 16 nodes

Table 6.9. Dynamic measurement of point-to-point communications with small problems (SIZE = S) on 16 nodes

program	type	number	number $\%$	volume	volume $\%$
	Static	0	0.0%	0	0.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	47104	100.0%	225 MB	100.0%
	Static	0	0.0%	0	0.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	6704	100.0%	7.83MB	100.0%
	Static	15	100.0%	0.06KB	100.0%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	0	0.0%	0	0.0%
BT	D. ana	23520	100.0%	209MB	100.0%
	Dynamic	0	0.0%	0	0.0%
SP	Static	0	0.0%	0	0.0%
	Dynamically analyzable	38880	100.0%	178 MB	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.9 shows the classification of point-to-point communications. As in the cases for large problems, we see more dynamic point-to-point communications than dynamic collective communications. CG and MG contain only dynamic point-to-point communications. BT and SP contain only dynamically analyzable point-to-point communications. It is even valid that none of the benchmarks has a significant number of static point-to-point communications. The distribution of static, dynamic, and dynamically analyzable point-to-point communications in these benchmarks does not change when executed with a smaller problem size.

Figure 6.4 shows the summary of the message size distribution for collective communications in all the benchmarks. The summary is obtained in the same manner as that for large problems. The benchmarks only have one dynamically analyzable communication, so there is not much distribution for that case. For dynamic collective communication, the message size has a range of 1KB-4KB, and for static ones, the message sizes are mostly small ($\leq 1KB$). A smaller problem size results in more small messages in collective communications. However, the trend in the message size distribution for small problems is similar to that for large problems.

Figure 6.5 shows the summary of the message size distribution for point-to-point communications in all the benchmarks. The summary is obtained in a similar manner to that of large problems. We also note that a smaller problem size results in smaller messages in point-to-point communications. However, the trend in the message size distribution for small problems is similar to that for large problems.



Figure 6.4. Message size distribution for collective communications (SIZE = S) on 16 nodes



Figure 6.5. Message size distribution for point-to-point communications (SIZE = S) on 16 nodes

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program	type	number	number $\%$	volume	volume $\%$
	Static	5	100.0%	$2.5 \mathrm{KB}$	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	0.0%	6.0B	0.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	6720	100.0%	746MB	100.0%
	Static	100	3.4%	25 KB	0.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	2856	96.6%	512MB	100.0%
	Static	3	27.3%	198B	0.0%
FT	Dynamically analyzable	8	72.7%	2.42GB	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	25	69.4%	272KB	0.1%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	30.6%	277MB	99.9%
	Static	18	0.0%	5.7KB	0.3%
LU	Dynamically analyzable	2016	1.6%	1.32GB	83.6%
	Dynamic	124008	98.4%	$254 \mathrm{MB}$	16.1%
	Static	7	0.1%	2.2KB	0.0%
BT	Dynamically analyzable	9672	99.9%	4.53GB	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	0.0%	2.2KB	0.0%
SP	Dynamically analyzable	19272	100.0%	7.90GB	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.10. Dynamic measurement for large problems (SIZE = A) on 4 nodes

Results for large problems on 4 nodes

6.3

Table 6.10 shows the dynamic measurement of the number and the volume for the three types of communications in each of the benchmarks. We can see from the table that the results show a similar trend as we have seen in the previous cases. In terms of the volume of communications, CG, MG, and IS are dominated by dynamic communications; EP contains only static communications; FT, BT, and SP are dominated by dynamically analyzable communications. LU has 83.6% dynamically analyzable communications, 16.1% dynamic communications, and a small percentage, 0.3%, of static communications. In general, using a smaller number of nodes increases the total communication volume, especially for point-to-point communications, but it does not significantly change the ratios among the volumes for static, dynamic, and dynamically analyzable communications.

program	type	number	volume	volume $\%$
EP	collective	5	$2.5 \mathrm{KB}$	100.0%
	point-to-point	0	0	0.0%
CG	collective	1	0.06B	0.0%
	point-to-point	6720	$746 \mathrm{MB}$	100.0%
MG	collective	100	$25.2 \mathrm{KB}$	0.0%
	point-to-point	2856	512 MB	100.0%
FT	collective	11	2.42 GB	100.0%
	point-to-point	0	0	0.0%
IS	collective	33	277 MB	100.0%
	point-to-point	3	0.01KB	0.0%
LU	collective	18	$5.72 \mathrm{KB}$	0.0%
	point-to-point	126024	1.58 GB	100%
BT	collective	7	2.22 KB	0.0%
	point-to-point	9672	$4.53 \mathrm{GB}$	100.0%
\overline{SP}	collective	7	2.22KB	0.0%
	point-to-point	19272	7.9GB	100.0%

Table 6.11. Dynamic measurement for collective and point-to-point communications with large problems (SIZE = A) on 4 nodes

Table 6.11 shows the number and the volume of collective and point-to-point communications in the benchmarks. We still obtain similar results: the communications in benchmarks EP, FT, and IS are dominated by collective communications while the communications in CG, MG, LU, BT, and SP are dominated by point-to-point communications. Using a smaller number of nodes does not significantly change the ratios between the volumes for collective and point-to-point communications.

Table 6.12 shows the classification of collective communications in the benchmarks. EP, CG, MG, LU, BT, and SP have collective communications that are all static while most of the collective communications in FT are dynamically analyzable. IS still have collective communications that are mostly dynamic. The collective communications in the benchmarks have a similar distribution among static, dynamic, and dynamically analyzable communications with different numbers of nodes in the system.

program	type	number	number $\%$	volume	volume $\%$
	Static	5	100.0%	$2.5 \mathrm{KB}$	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	100.0%	0.03KB	100.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	100	100.0%	$25.2 \mathrm{KB}$	100.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	3	27.3%	$0.20 \mathrm{KB}$	0.0%
FT	Dynamically analyzable	8	72.7%	2.42 GB	100%
	Dynamic	0	0.0%	0	0.0%
	Static	22	66.7%	272 KB	0.1%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	33.3%	278 MB	99.9%
	Static	18	100.0%	$5.72 \mathrm{KB}$	100.0%
LU	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	100.0%	2.22 KB	100.0%
BT	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
SP	Static	7	100.0%	2.22 KB	100.0%
	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.12. Dynamic measurement of collective communications with large problems (SIZE = A) on 4 nodes

Results of point-to-point classification are shown in Table 6.13. Again, CG and MG contain only dynamic point-to-point communications whereas BT and SP contain only dynamically analyzable point-to-point communications. None of the benchmarks has a significant number of static point-to-point communications. A smaller number of nodes does not significantly change the distribution of static, dynamic, and dynamically analyzable point-to-point communications in these benchmarks.

The summary of the message size distribution for collective communications in all the benchmarks is shown in Figure 6.6. This figure shows almost identical results to patterns when the benchmarks are run on 16 nodes with a large problem size.

program	type	number	number $\%$	volume	volume $\%$
	Static	0	0.0%	0	0.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	6720	100.0%	746MB	100.0%
	Static	0	0.0%	0	0.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	2856	100.0%	512 MB	100.0%
	Static	3	100.0%	0.01KB	100.0%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	0	0.0%	0	0.0%
LU	Dynamically analyzable	2016	1.6%	1.32 GB	83.9%
	Dynamic	124008	98.4%	254 MB	16.1%
	Static	0	0.0%	0	0.0%
BT	D. ana	9672	100.0%	$4.53 \mathrm{GB}$	100.0%
	Dynamic	0	0.0%	0	0.0%
SP	Static	0	0.0%	0	0.0%
	Dynamically analyzable	19272	100.0%	7.9GB	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.13. Dynamic measurement of point-to-point communications with large problems (SIZE = A) on 4 nodes



Figure 6.6. Message size distribution for collective communications (SIZE = A) on 4 nodes



Figure 6.7. Message size distribution for point-to-point communications (SIZE = A) on 4 nodes

The message sizes for dynamic and dynamically analyzable communications become larger, but the message size distribution has a similar trend. Figure 6.7 shows the summary of the message size distribution for point-to-point communications in all the benchmarks. With a smaller number of nodes, more messages are of larger sizes. However, the message size distribution shows a similar trend: the static point-to-point communications have a small message size while dynamic and dynamically analyzable point-to-point communications generally have medium to large message sizes.

6.4 Results for small problems on 4 nodes

Table 6.14 shows the dynamic measurement of the number and the volume for the three types of communications in each of the benchmarks. The table, in accordance to previous experiments, reveals the same trend as we had before, although the communication volume is significantly smaller. LU has 0.1% static communications,

program	type	number	number %	volume	volume $\%$
	Static	5	100.0%	2.5KB	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	0.0%	6.0B	0.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	6720	100.0%	74.7MB	100.0%
	Static	100	5.3%	25 KB	0.3%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	1776	94.7%	9MB	99.7%
	Static	3	27.3%	198B	0.0%
FT	Dynamically analyzable	8	72.7%	$75.5 \mathrm{MB}$	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	25	69.4%	137KB	6.0%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	30.6%	2.16MB	94.0%
	Static	18	0.4%	$5.7 \mathrm{KB}$	0.1%
LU	Dynamically analyzable	416	9.4%	$9.58 \mathrm{MB}$	86.1%
	Dynamic	4008	90.2%	$1.54 \mathrm{MB}$	13.8%
	Static	7	0.2%	$2.2 \mathrm{KB}$	0.0%
BT	Dynamically analyzable	2952	99.8%	$57.3 \mathrm{MB}$	100.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	0.1%	$2.2 \mathrm{KB}$	0.0%
SP	Dynamically analyzable	4872	99.9%	59.2MB	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.14. Dynamic measurement for small problems (SIZE = S) on 4 nodes

86.1% dynamically analyzable communications, and 13.8% dynamic communications in terms of the volume of communication. CG, MG, and IS are still dominated by dynamic communications; EP contains only static communications; FT, BT, and SP are dominated by dynamically analyzable communications.

We show the number and the volume of collective and point-to-point communications for each benchmarks in Table 6.15. The table also shows the same trend as we had in previous executions with different problem sizes and different numbers of nodes. The communications in benchmarks EP, FT, and IS are dominated by collective communications while the communications in CG, MG, LU, BT, and SPare dominated by point-to-point communications.

program	type	number	volume	volume $\%$
EP	collective	5	$2.5 \mathrm{KB}$	100.0%
	point-to-point	0	0	0.0%
CG	collective	1	0.06B	0.0%
	point-to-point	6720	74.7MB	100.0%
MG	collective	100	$25.2 \mathrm{KB}$	0.3%
	point-to-point	1776	9.00MB	99.7%
FT	collective	11	$75.5 \mathrm{MB}$	100.0%
	point-to-point	0	0	0.0%
IS	collective	33	$2.3 \mathrm{MB}$	100.0%
	point-to-point	3	0.01KB	0.0%
LU	collective	18	$5.72 \mathrm{KB}$	0.0%
	point-to-point	4424	11.1MB	100%
BT	collective	7	$2.22 \mathrm{KB}$	0.0%
	point-to-point	2952	$57.3 \mathrm{MB}$	100.0%
\overline{SP}	collective	7	2.22 KB	0.0%
	point-to-point	4872	$59.2 \mathrm{MB}$	100.0%

Table 6.15. Dynamic measurement for collective and point-to-point communications with small problems (SIZE = S) on 4 nodes

program	type	number	number $\%$	volume	volume $\%$
	Static	5	100.0%	$2.5 \mathrm{KB}$	100.0%
EP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	1	100.0%	0.03KB	100.0%
CG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	100	100.0%	$25.2 \mathrm{KB}$	100.0%
MG	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	3	27.3%	$0.20 \mathrm{KB}$	0.0%
FT	Dynamically analyzable	8	72.7%	$75.5 \mathrm{MB}$	100%
	Dynamic	0	0.0%	0	0.0%
	Static	22	66.7%	137KB	6.0%
IS	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	11	33.3%	$2.16 \mathrm{MB}$	94.0%
	Static	18	100.0%	$5.72 \mathrm{KB}$	100.0%
LU	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	100.0%	2.22 KB	100.0%
BT	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
	Static	7	100.0%	$2.22 \mathrm{KB}$	100.0%
SP	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.16. Dynamic measurement of collective communications with small problems (SIZE = S) on 4 nodes

Table 6.16 shows the classification of collective communications in the benchmarks. Even this table shows a similar trend as in other collective communications tables before. Among the benchmarks, EP, CG, MG, LU, BT, and SP have collective communications that are all static. One benchmark, FT, had collective communications that are dynamically analyzable. Only the collective communications in IS are mostly dynamic.

Table 6.17 shows the classification of point-to-point communications. The trend in this table is similar to that in previous results: none of the benchmarks has a significant number of static point-to-point communications; CG and MG contain

program	type	number	number $\%$	volume	volume $\%$
CG	Static	0	0.0%	0	0.0%
	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	6720	100.0%	74.7MB	100.0%
MG	Static	0	0.0%	0	0.0%
	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	1776	100.0%	9.00MB	100.0%
IS	Static	3	100.0%	0.01KB	100.0%
	Dynamically analyzable	0	0.0%	0	0.0%
	Dynamic	0	0.0%	0	0.0%
LU	Static	0	0.0%	0	0.0%
	Dynamically analyzable	416	9.40%	9.59MB	86.2%
	Dynamic	4008	90.6%	$1.54 \mathrm{MB}$	13.8%
BT	Static	0	0.0%	0	0.0%
	D. ana	2952	100.0%	$57.3 \mathrm{MB}$	100.0%
	Dynamic	0	0.0%	0	0.0%
SP	Static	0	0.0%	0	0.0%
	Dynamically analyzable	4872	100.0%	$59.2 \mathrm{MB}$	100.0%
	Dynamic	0	0.0%	0	0.0%

Table 6.17. Dynamic measurement of point-to-point communications with small problems (SIZE = S) on 4 nodes

only dynamic point-to-point communications; BT and SP contain only dynamically analyzable point-to-point communications.

Figure 6.8 shows the summary of the message size distribution for collective communications in all the benchmarks. The benchmarks have only one large message size (1MB+) for dynamically analyzable communication, so there is not much distribution for the dynamically analyzable case. About 95% of the messages for dynamic communications are in the range of 16KB-64KB while 5% are in the range of 4KB-16KB. For static collective communications, the message sizes are mostly small (< 1KB). Figure 6.9 shows the summary of the message size distribution for point-to-point communications in all the benchmarks. As in previous results, the static point-to-point communications have a small message size while dynamic and dynamically analyzable point-to-point communications generally have medium to large message sizes.



Figure 6.8. Message size distribution for collective communications (SIZE = S) on 4 nodes



Figure 6.9. Message size distribution for point-to-point communications (SIZE = S) on 4 nodes

CHAPTER 7

CONCLUSIONS

We studied the communication characteristics in the MPI implementation of the NAS parallel benchmarks and investigated the feasibility and effectiveness of compiled communication on MPI programs. The results of this study can also be used by other compiler assisted approaches to improve communication performance. The main conclusions are the followings:

- Static and dynamically analyzable communications account for a significant portion of the communications in the benchmarks, which indicates that compiled communication can be effective if it can optimize these two types of communications.
- The majority of collective communications are static, which indicates that compiled communication should be applied to optimize MPI collective communications. Furthermore, most static collective communications have small message sizes.
- There is a significant number of dynamically analyzable point-to-point communications in the benchmarks. For compiled communication to be effective in handling MPI point-to-point communications, it must be able to optimize dynamically analyzable communications.
- While different problem sizes and different numbers of nodes in the system affect the sizes of messages in the communications, they do not significantly

change the distribution and the ratio of static, dynamic, and dynamically analyzable communications in the benchmarks. Thus, the above conclusions hold for different problem sizes and different numbers of nodes in the system.

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BIOGRAPHICAL SKETCH

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