

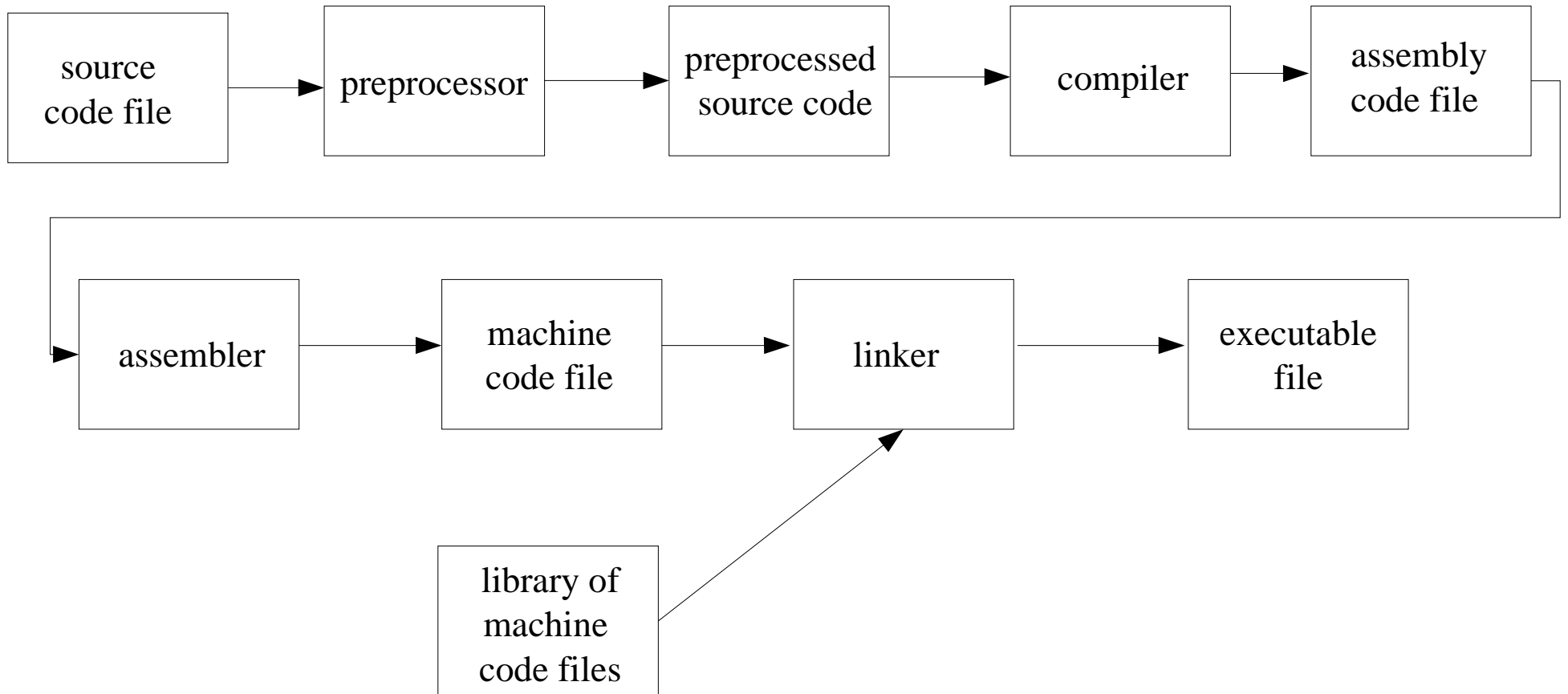
Branch Elimination via Multi-Variable Condition Merging

William Krehling

Outline of Presentation

- **Background and tools.**
- Introduce technique for multi-variable condition merging.
- Rules for merging multiple variables.
- Describe framework for performing the analysis.
- Results & Conclusion.

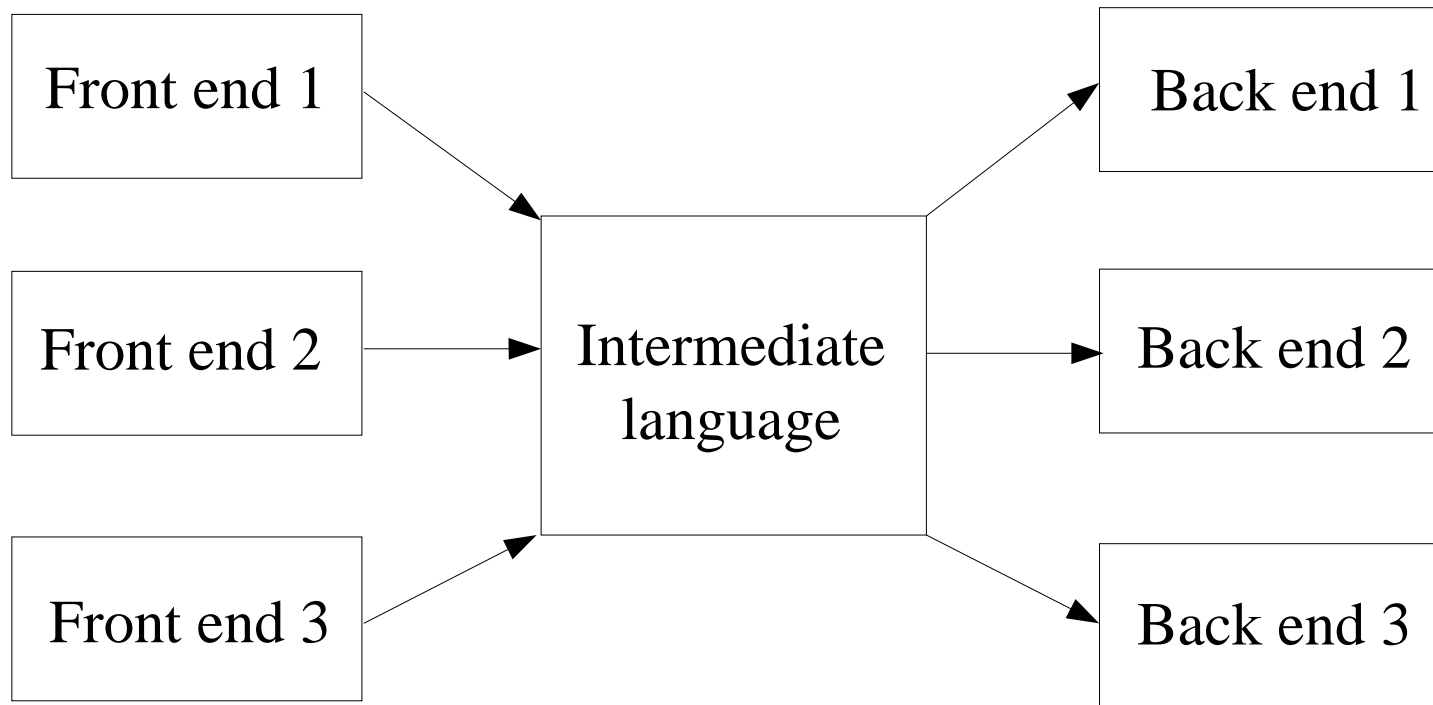
General Compilation Process



Front and Back Ends

- Front end
 - takes high-level source code as input
 - produces intermediate code as output
- Back end
 - takes intermediate code as input
 - produces assembly or machine code

Intermediate Language



Very Portable Optimizer (VPO)

- Research Compiler
- Very simple front end
- Translates source code into intermediate language.

Register Transfer Lists

- “Generic assembly language”
- Used by many compilers including GCC.
- All transformations in VPO done at the RTL level.

Example RTLs

- $r[2] = r[4]$ -- move
- $r[5] = r[6] + r[7]$ -- add add r5,r6,r7
- $M[r[2] + 4] = r[3]$ -- store
- $IC = r[2] ? r[3]$ -- comparison

Outline of Presentation

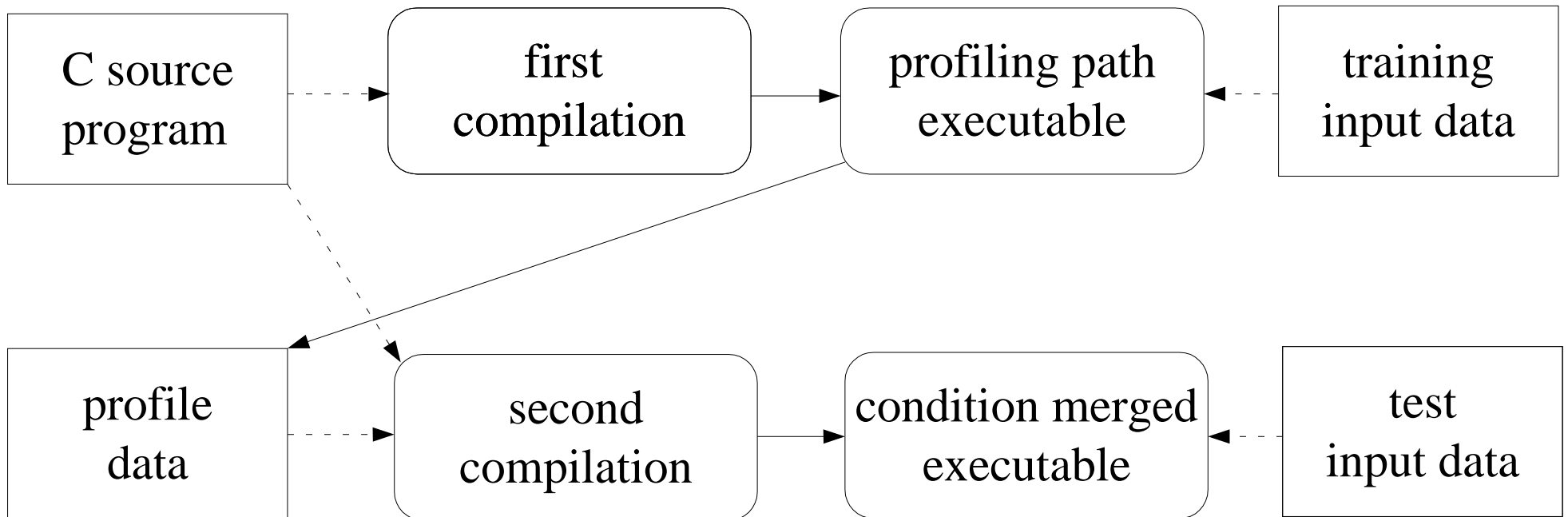
- Background and tools.
- **Introduce technique for multi-variable condition merging.**
- Rules for merging multiple variables.
- Describe framework for performing the analysis.
- Results & Conclusion.

Motivation

- The execution of conditional branches is expensive.
- Causes pipeline flushes.
- Inhibits other code improving transformations.

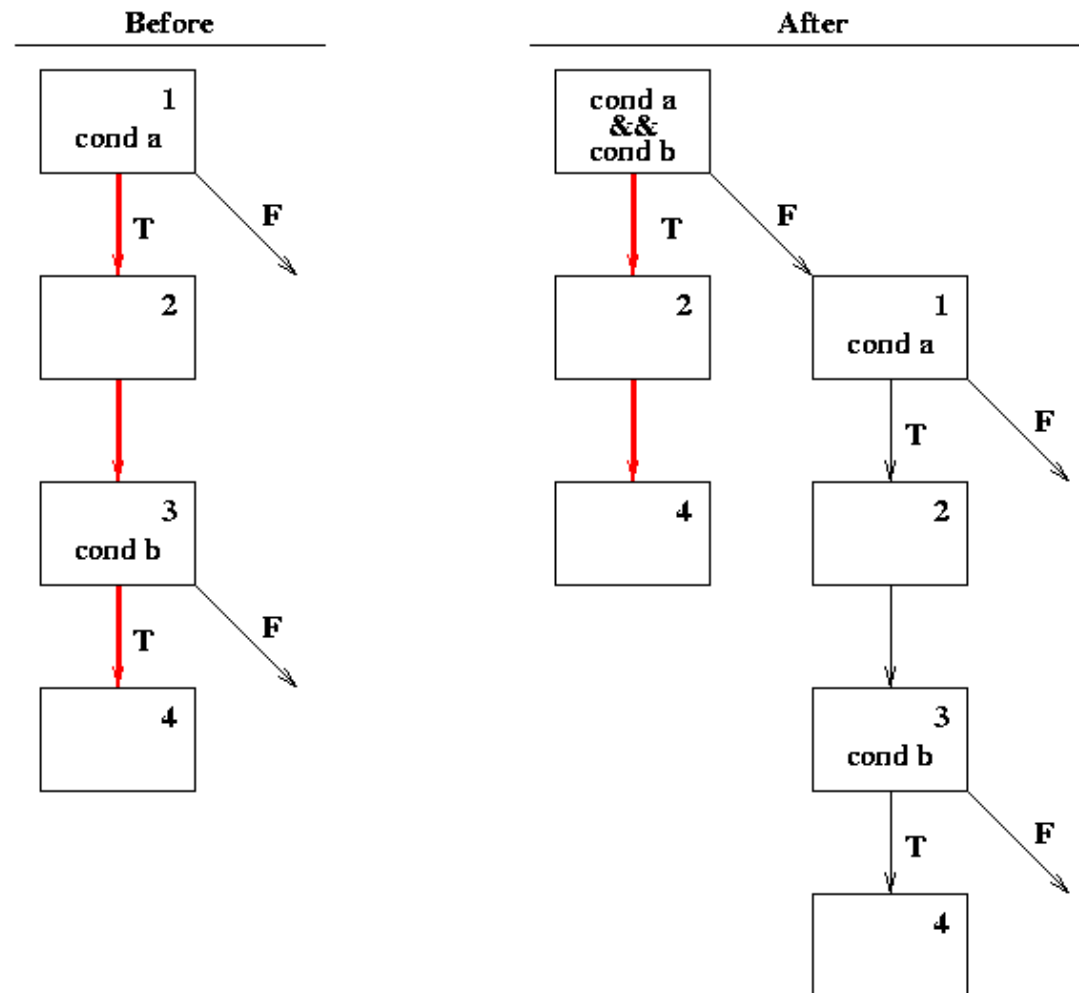


Compilation Process for Condition Merging



Condition Merging

- Merging branches means replacing the execution of two or more branches with the execution of a single branch.



Tests Involving Multiple Variables

- How can conditions that test the results of comparisons of multiple variables be merged?

Tests Involving Multiple Variables

- How can conditions that test the results of comparisons of multiple variables be merged?
 - Consider comparisons to zero.
 - Consider the use of logical operations.

Tests Involving Multiple Variables (Equal to Zero)

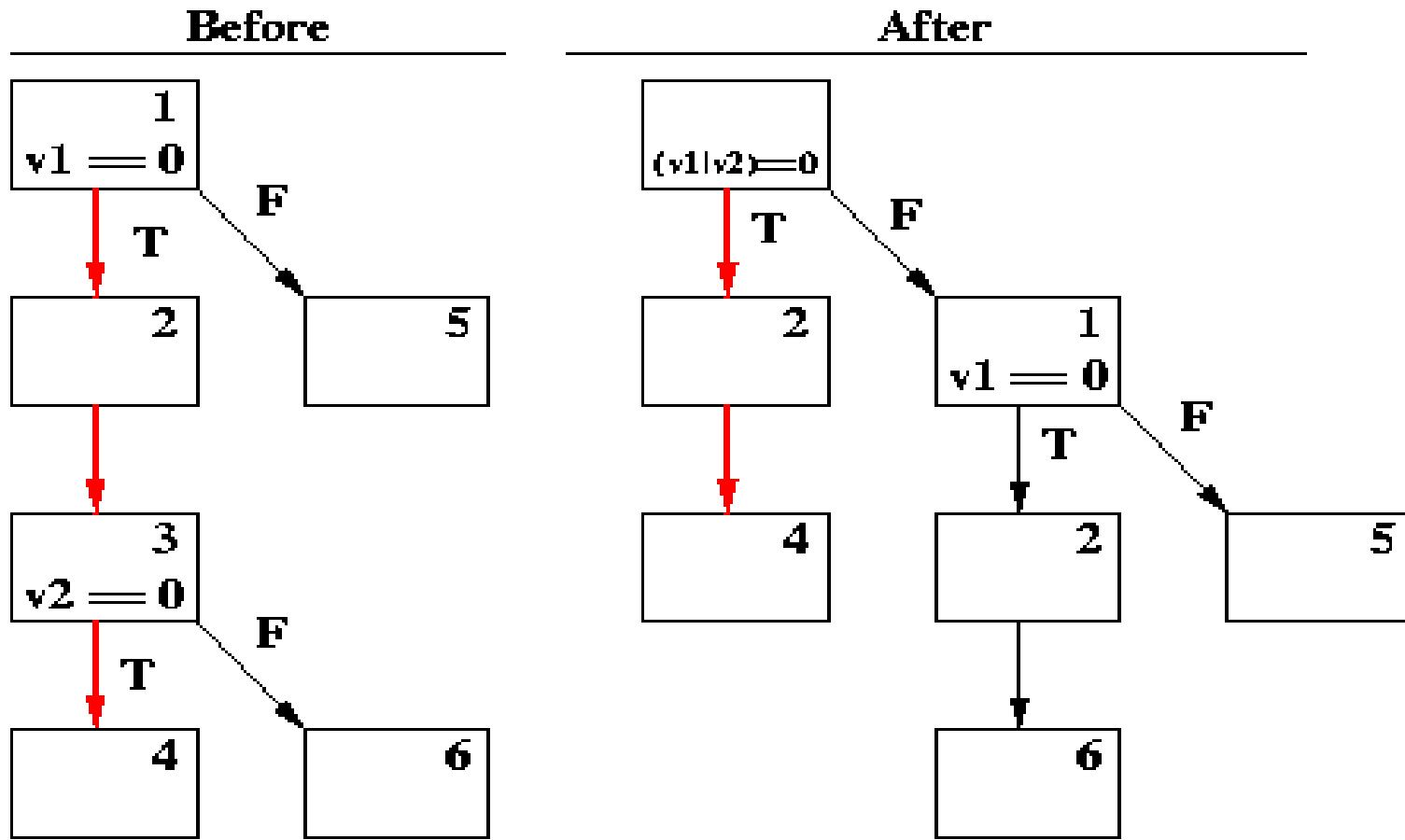
`v1==0 && v2==0` \leftrightarrow ??

Tests Involving Multiple Variables (Equal to Zero)

$$v1==0 \ \&\& \ v2==0 \ \leftrightarrow \ (v1|v2)==0$$

Tests Involving Multiple Variables (Equal to Zero)

$$v1 == 0 \ \&\& \ v2 == 0 \ \leftrightarrow \ (v1 | v2) == 0$$



Checking If Multiple Variables Are Equal to Zero (cont.)

- n sets of compares and branches are replaced by n-1 logical operations and 1 branch

```
r[t]=r[1]|r[2];
```

```
r[t]=r[t]|r[3];
```

```
...
```

```
IC=(r[t]|r[n])?0;
```

```
PC=IC!=0,<bypass target>;
```

Outline of Presentation

- Background and tools.
- Introduce technique for multi-variable condition merging.
- **Rules for merging multiple variables.**
- Describe framework for performing the analysis.
- Results & Conclusion.

Merging Conditions Comparing Multiple Variables to 0 or -1

`v1 == 0 && v2 == 0` \leftrightarrow `(v1 | v2) == 0`

`v1 == 0 && v2 == -1` \leftrightarrow

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \iff (v1 \mid v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \iff (v1 \mid \sim v2) == 0$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \ \leftrightarrow \ (v1 \mid v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \ \leftrightarrow \ (v1 \mid \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \ \leftrightarrow$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \ \leftrightarrow \ (v1 \ | \ v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \ \leftrightarrow \ (v1 \ | \ \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \ \leftrightarrow \ (v1 \& \ v2) < 0$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \ \leftrightarrow \ (v1 \ | \ v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \ \leftrightarrow \ (v1 \ | \ \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \ \leftrightarrow \ (v1 \ \& \ v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 >= 0 \ \leftrightarrow$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \iff (v1 \mid v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \iff (v1 \mid \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \iff (v1 \& v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 >= 0 \iff (v1 \mid v2) >= 0$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \ \leftrightarrow \ (v1 \ | \ v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \ \leftrightarrow \ (v1 \ | \ \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \ \leftrightarrow \ (v1 \ \& \ v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 >= 0 \ \leftrightarrow \ (v1 \ | \ v2) >= 0$$

$$v1 < 0 \ \&\& \ v2 >= 0 \ \leftrightarrow$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \iff (v1 \mid v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \iff (v1 \mid \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \iff (v1 \& v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 >= 0 \iff (v1 \mid v2) >= 0$$

$$v1 < 0 \ \&\& \ v2 >= 0 \iff (v1 \& \sim v2) < 0$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \ \leftrightarrow \ (v1 \ | \ v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \ \leftrightarrow \ (v1 \ | \ \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \ \leftrightarrow \ (v1 \& \ v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 >= 0 \ \leftrightarrow \ (v1 \ | \ v2) >= 0$$

$$v1 < 0 \ \&\& \ v2 >= 0 \ \leftrightarrow \ (v1 \& \ \sim v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 < 0 \ \leftrightarrow$$

Merging Conditions Comparing Multiple Variables to 0 or -1

$$v1 == 0 \ \&\& \ v2 == 0 \iff (v1 \mid v2) == 0$$

$$v1 == 0 \ \&\& \ v2 == -1 \iff (v1 \mid \sim v2) == 0$$

$$v1 < 0 \ \&\& \ v2 < 0 \iff (v1 \& v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 >= 0 \iff (v1 \mid v2) >= 0$$

$$v1 < 0 \ \&\& \ v2 >= 0 \iff (v1 \& \sim v2) < 0$$

$$v1 >= 0 \ \&\& \ v2 < 0 \iff (v1 \mid \sim v2) >= 0$$

Are Multiple Variables \neq to Zero?

- How can we detect if n variables are all not equal to zero in a single branch?

Are Multiple Variables \neq to Zero?

- How can we detect if n variables are all not equal to zero in a single branch?
 - Are one or more bit positions in all of the variables set?

$$(v1 \& v2) \neq 0 \rightarrow v1 \neq 0 \ \&\& \ v2 \neq 0$$

Are Multiple Variables != to Zero?

- How can we detect if n variables are all not equal to zero in a single branch?

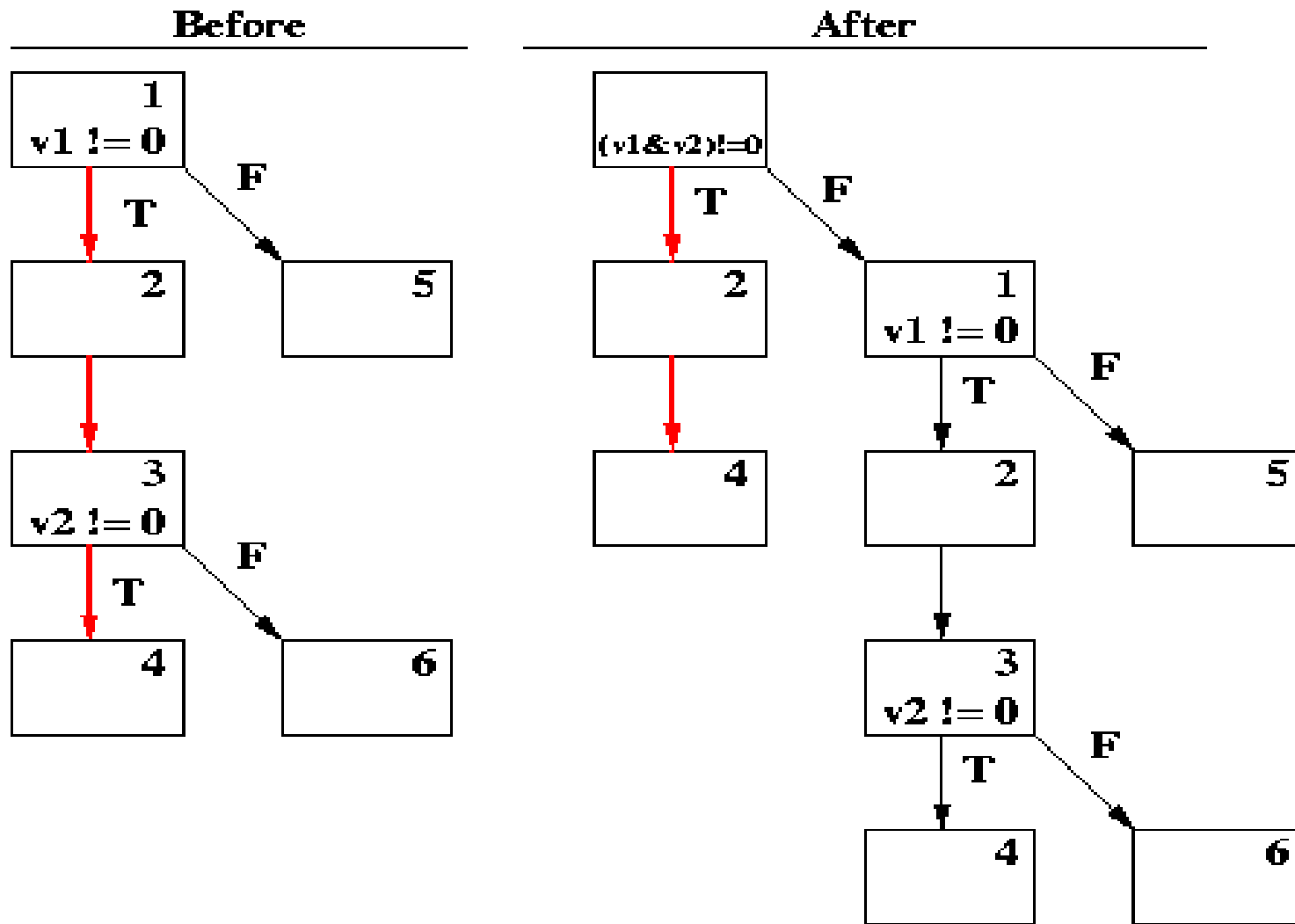
- Are one or more bit positions in all of the variables set?

$(v1 \& v2) \neq 0 \rightarrow v1 \neq 0 \ \&\& \ v2 \neq 0$

- example:

`if (p1 && p2 && p1->val == p2->val)`

Checking If Multiple Variables Are Not Equal to Zero (cont.)



Checking If Multiple Variables Are Not Equal to Multiple Constants

- How can we check if n variables are all not equal to n constants in a single branch?

Checking If Multiple Variables Are Not Equal to Multiple Constants (cont.)

- Is a bit position set in all of the variables and is the same bit position clear in all of the constants?

$$(v1 \& v2) \& \sim (c1 | c2) \neq 0 \rightarrow v1 \neq c1 \ \&\& \ v2 \neq c2$$

- Say $v1=6$, $v2=10$, $c1=9$, and $c2=5$

- $(0110_2 \& 1010_2) \& \sim(1001_2 | 0101_2) =$

$$(0010_2) \& \sim(1101_2) = (0010_2) \& (0010_2) = 0010_2 \neq 0$$

Checking If Multiple Variables Are Not Equal to Multiple Constants (cont.)

- Consider the case where the constants are all zero.

$(v1 \& v2) \& \sim (c1 | c2) \neq 0 \rightarrow v1 \neq c1 \ \&\& \ v2 \neq c2$

$(v1 \& v2) \& \sim (0 | 0) \neq 0$

$(v1 \& v2) \& 0\text{xFFFFFFFF} \neq 0$

$(v1 \& v2) \neq 0$

Checking If Multiple Variables Are Not Equal to Multiple Constants (cont.)

- Is a bit position clear in all of the variables and is the same bit position set in all of the constants?

$$\sim(v1 | v2) \& (c1 \& c2) \neq 0 \rightarrow v1 \neq c1 \ \&\& \ v2 \neq c2$$

- Say $v1=6$, $v2=10$, $c1=9$, and $c2=5$

- $\sim(0110_2 | 1010_2) \& (1001_2 \& 0101_2) =$

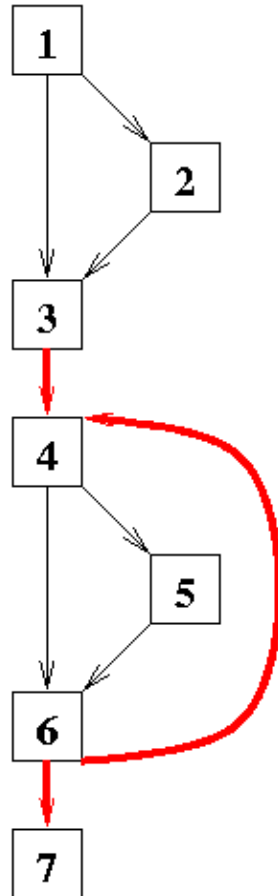
$$\sim(1110_2) \& (0001_2) = (0001_2) \& (0001_2) = 0001_2 \neq 0$$

Outline of Presentation

- Background and tools.
- Introduce technique for multi-variable condition merging.
- Rules for merging multiple variables.
- **Describe framework for performing the analysis.**
- Results & Conclusion.

Framework for Obtaining Path Profile Information

- Detect paths dynamically during a profile run.
- Paths do not cross loop boundaries.



Using the Path Profile Information

- Accumulate statistics and estimate the benefit to merge each set.
 - likelihood that the path will be taken given that the first branch is reached
 - instructions executed if the dominant path is taken
 - instructions executed if the dominant path is not taken
- Merge sets in the order of the most beneficial sets of branches first.

Using the Path Profile Information

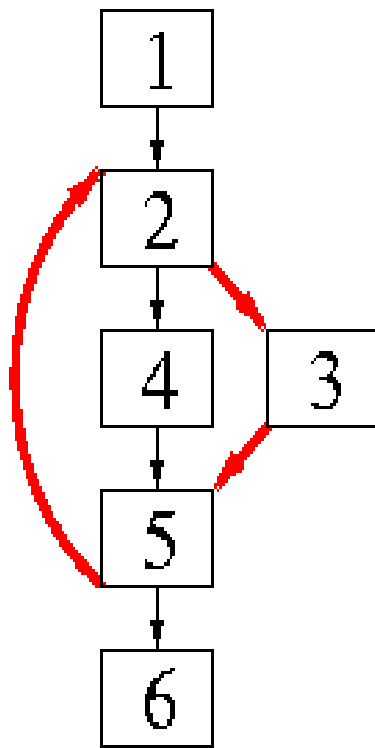
- Rely on other optimizations to improve the modified code.
 - loop-invariant code motion
 - common subexpression elimination

Paths Across Loop Boundaries

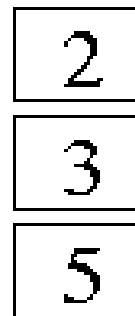
- During profile run, detect a frequently executed path, that is followed by itself.
- Insert a new path into the data structure.
 - The original path, with every block duplicated.
 - Treated as a separate and distinct path.

Paths Across Loop Boundaries

Loop



Frequently executed path



Duplicate path



Choosing Which Branches to Merge

- Once we have detected all the paths, we examine them for mergeable branches and collect these into sets.
- Just because a set is valid, does not mean it would be beneficial to actually merge.
- Possible that the same sets of mergeable branches will have been detected by more than one of the rules.

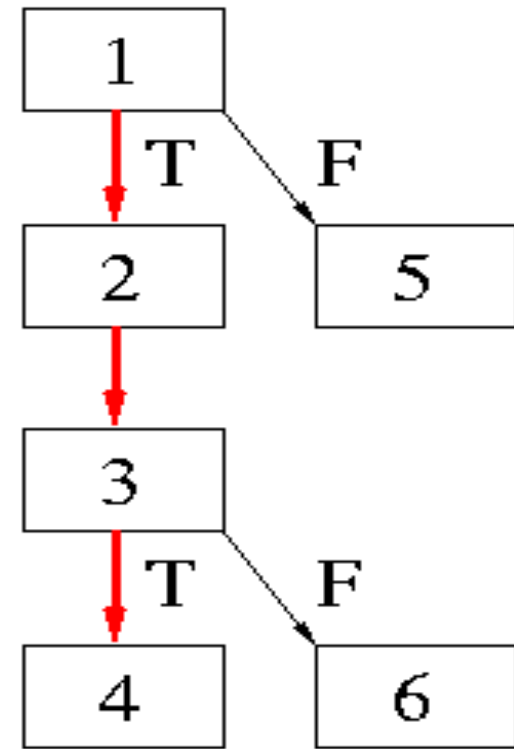
Choices Driven by Estimates

- Have to estimate the benefit from merging a set of branches.
- Generalized formula:
$$((\text{win path ratio} * \text{saved instructions}) - (\text{lose path ratio} * \text{added instructions})) * \text{total execution when the path is reached.}$$

Win/Lose/Breakeven Paths

- Once we have picked a set, we must duplicate code with the new merged branches and their targets.
- With many paths we will create a win path, a lose path, and a breakeven path.

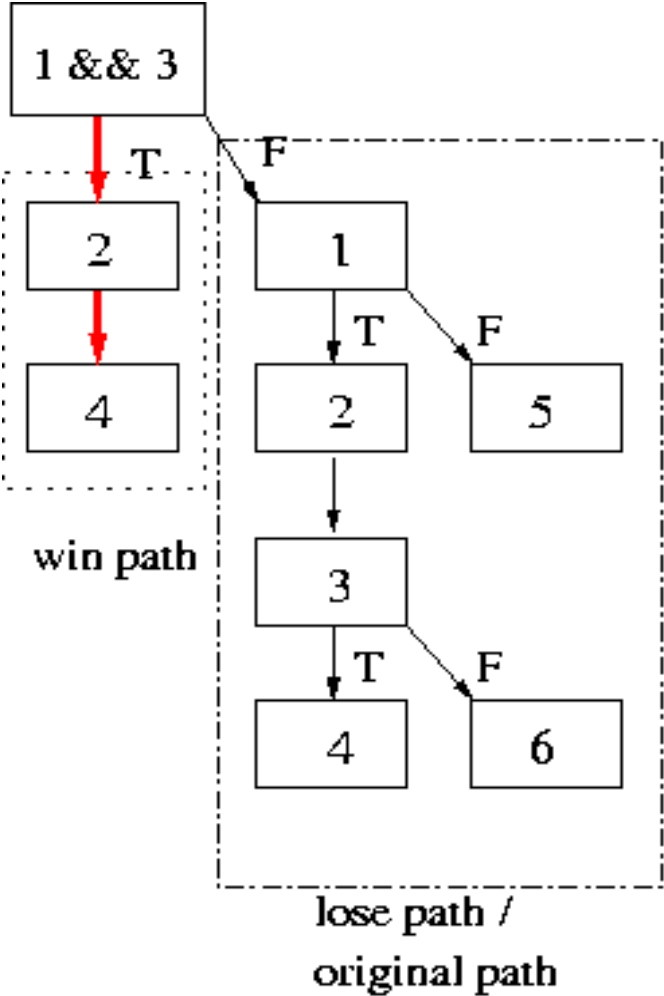
Example Win/Lose/Breakeven Path



original path

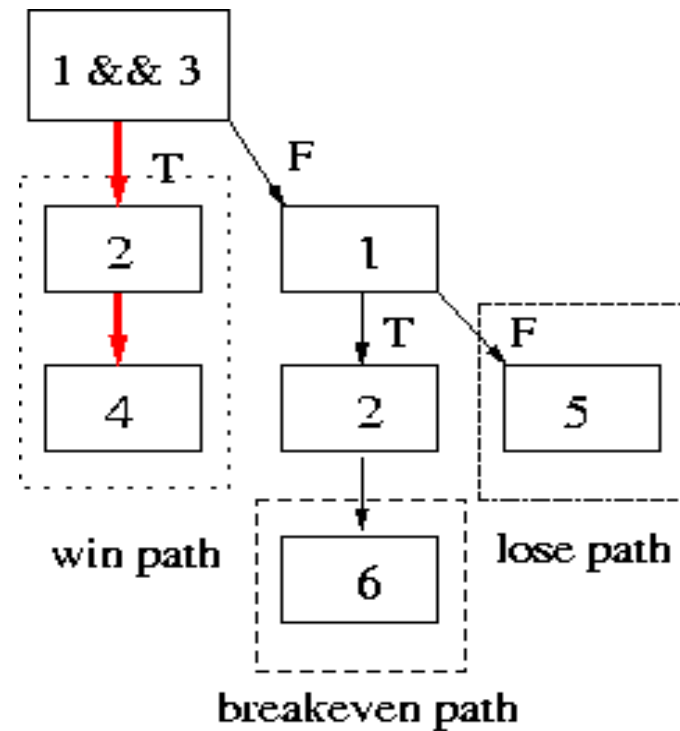
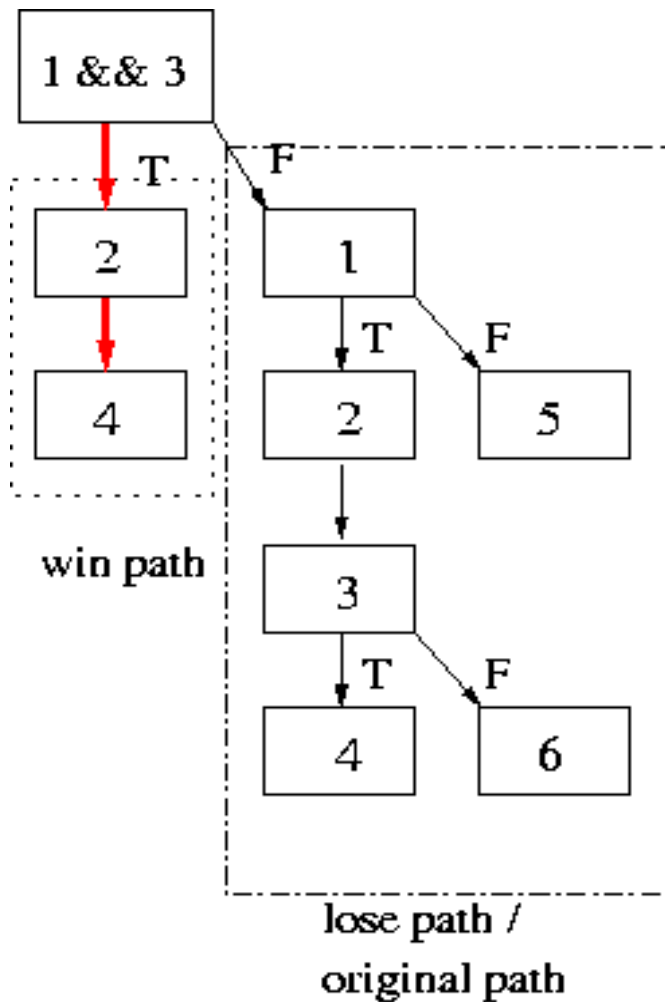
Reach block 6 (original 2)

Example Win/Lose/Breakeven Path



Reach block 6 (original 2) (lose 3)

Example Win/Lose/Breakeven Path



Reach block 6 (original 2) (lose 3)
(breakeven 2)

Outline of Presentation

- Background and tools.
- Introduce technique for multi-variable condition merging.
- Rules for merging multiple variables.
- Describe framework for performing the analysis.
- **Results & Conclusion.**

Results



Conclusions

- Contributions
 - Able to merge conditions involving multiple variables on a conventional scalar processor.
 - Obtained benefits by merging conditions in paths that are not the most frequent.

Conclusions

- Contributions
 - Able to merge conditions involving multiple variables on a conventional scalar processor.
 - Obtained benefits by merging conditions in paths that are not the most frequent.

Acknowledgments

- Dr. David Whalley
- Dr. Mark Bailey
- Dr. Xin Yuan
- Dr. Gang-Ryung Uh
- Dr. Robert van Engelen

Publications

- “Branch Elimination by Condition Merging” by W. Krehling et. al., in *Software Practice and Experience*, 35(1), PP 51-74, January 2005.
- “Branch Elimination via Multi-Variable Condition Merging” by W. Krehling et. al., in *The Proceedings of the Euro-Par '03 Conference on Parallel Processing*, PP 261-270, August 2003.

Current Research

- Reducing Branch costs using “Implicit Comparisons”.
- Hardware modifications.
- New instructions to decouple the comparison definition from the actual comparison of values.