

Functions for extracting information from i^{th} instruction of program number i .

Input of functions: $\#$ value i for i^{th} instruction.

y is the program $\#$.

Recall that program $\#$ y is created as follows:

$$[\#I_1, \#I_2, \dots, \#I_n] - 1 = \#P = y$$

Hence $(y+1)i$ is the value or number of the i^{th} instruction. That is, it is some

$\langle a, \langle b, c \rangle \rangle$ for the i^{th} instruction

$$\text{Label}(i, y) = l((y+1)i)$$

This is the value ^{"a"} of any label in the set of labels. If no label it is 0.

$$\text{Var}(i, y) = r(r((y+1)i)) + 1$$

This is the index $\#$ of the variable of the instruction. Note that it was necessary to get $\langle b, c \rangle$ first, then "c" and then add 1 to that value "c".

$$\text{INSTR}(i, y) = l(r((y+1)i))$$

This is the value of b . Note it can be 0, 1, 2, or higher if it is a label pointer for IF inst.

$$\text{LABEL}'(i, y) = l(r((y+1)i)) \div 2$$

The value of the actual label $\#$, or 0 if it is a substruct inst.

A snapshot has 2 ~~two~~ values. The index of the instruction to be executed, say i . Also, the state of the computation or values for all variables. We originally used $\langle i, \sigma \rangle$ for a snapshot. We now use $\langle i, s \rangle$ for a snapshot. This "number" is using pairing

Here i is the instruction #. However s is a number representing the state of the computation. Hence it is the #

$$s = \prod_{i=1}^n p_i^{x_i} \quad \text{for all indices } i \text{ of variables that have nonzero values.}$$

We then create the "pair" value $x = \langle i, s \rangle$

The next set of predicates relate to this x , and program γ .

- SKIP(x, y) : this predicate and other predicates
- INCR(x, y)
- DECR(x, y)
- BRANCH(x, y) operate on the same x, y as above.

VAR($l(x), y$) is: the index of the variable in the current instruction i .

PVAR(l) is: the prime # in s whose exponent in the current value of the variable

$\nu(x)$ is: the value $s = \prod_{i=1}^n p_i^{x_i}$

PVAR($l(x), y$) | $\nu(x)$ means the values of ν_i divides s .

SKIP (x,y) : It is true if the instruction value b in $\langle a, \langle b, c \rangle \rangle = 0$, or if if the value $b \geq 2$ and the index value of label has value 0 .

INCR (x,y) : need to do an add

DECR (x,y) : need to do a subtract \Rightarrow value of variable is ≥ 1 .

BRANCH (x,y) : if \exists a value of a label to branch to.

Note $x = \langle i, S \rangle$ is the snapshot
 $y = \text{program \#}$ $l(x)$ is i

SKIP(x,y) $b = 0 \ \& \ i = \text{Lt}(\text{program})$
 $\vee b \geq 0 \ \& \ \underbrace{\sim (p_i \mid S)}_{\text{value of variable is } 0}$ } goto next instruction

INCR(x,y) $b = 1$

DECR(x,y) $b = 2 \ \& \ \text{value of variable is not } 0.$

BRANCH(x,y) $b > 2 \ \& \ \text{variable} \neq 0$
 $\& \ \text{the next label \# LABEL' is one of the labels in the program.}$

[Predicates above]

SUCC(x,y) = { gives the next snapshot.
 otherwise the instruction right after program ends

define next snapshot

initial snapshot $\rightarrow \text{INIT}^{(n)}(x_1, \dots, x_n) = \langle 1, \prod_{i=1}^n (p_{2i})^{x_i} \rangle$

Predicate $\rightarrow \text{TERM}(x,y)$ is x a terminal snapshot

$\text{SNAP}(x_1, \dots, x_n, y, 0) = \text{INIT}(x_1, \dots, x_n)$

\downarrow sequence of snapshots by number. $0^k, 1, 2, 3, \dots$

$\text{STP}^{(n)}(x_1, \dots, x_n, y, t) \Leftrightarrow \text{TERM}(\text{SNAP}(x_1, \dots, x_n, y, t); y)$