

Functions for extracting information from  $i^{\text{th}}$  instruction of program number  $i$ .

Input of functions:  $\#$  value  $i$  for  $i^{\text{th}}$  instruction.

$y$  is the program  $\#$ .

Recall that program  $\# y$  is created as follows:

$$[\#I_1, \#I_2, \dots, \#I_n] - 1 = \#P = y$$

Hence  $(y+1)i$  is the value or number of the  $i^{\text{th}}$  instruction. That is, it is some

$\langle a, \langle b, c \rangle \rangle$  for the  $i^{\text{th}}$  instruction

$$\text{Label}(i, y) = l((y+1)i)$$

This is the value <sup>"a"</sup> of any label in the set of labels. If no label it is 0.

$$\text{Var}(i, y) = r(r((y+1)i)) + 1$$

This is the index  $\#$  of the variable of the instruction. Note that it was necessary to get  $\langle b, c \rangle$  first, then "c" and then add 1 to that value "c".

$$\text{INSTR}(i, y) = l(r((y+1)i))$$

This is the value of  $b$ . Note it can be 0, 1, 2, or higher if it is a label pointer for IF inst.

$$\text{LABEL}'(i, y) = l(r((y+1)i)) \div 2$$

The value of the actual label  $\#$ , or 0 if it is a substart inst.

A snapshot has 2 ~~two~~ values. The index of the instruction to be executed, say  $i$ . Also, the state of the computation or values for all variables. We originally used  $\langle i, \sigma \rangle$  for a snapshot. We now use  $\langle i, s \rangle$  for a snapshot. This "number" is using pairing

Here  $i$  is the instruction #. However  $s$  is a number representing the state of the computation. Hence it is the #

$$s = \prod_{i=1}^n p_i^{x_i} \quad \text{for all indices } i \text{ of variables that have nonzero values.}$$

We then create the "pair" value  $x = \langle i, s \rangle$

The next set of predicates relate to this  $x$ , and program  $\gamma$ .

- SKIP( $x, y$ ) : this predicate and other predicates
- INCR( $x, y$ )
- DECR( $x, y$ )
- BRANCH( $x, y$ ) operate on the same  $x, y$  as above.

VAR( $l(x), y$ ) is: the index of the variable in the current instruction  $i$ .

PVAR( $l$ ) is: the prime # in  $s$  whose exponent in the current value of the variable

$\nu(x)$  is: the value  $s = \prod_{i=1}^n p_i^{x_i}$

PVAR( $l(x), y$ ) |  $\nu(x)$  means the values of  $\nu_i$  divides  $s$ .

SKIP (x,y) : It is true if the instruction value  $b$  in  $\langle a, \langle b, c \rangle \rangle = 0$ , or if if the value  $b \geq 2$  and the index value of label has value  $0$ .

INCR (x,y) : need to do an add

DECR (x,y) : need to do a subtract  $\Rightarrow$  value of variable is  $\geq 1$ .

BRANCH (x,y) : if  $\exists$  a value of a label to branch to.