

CIS 4360, SPRING 2026

HASH FUNCTION

VIET TUNG HOANG

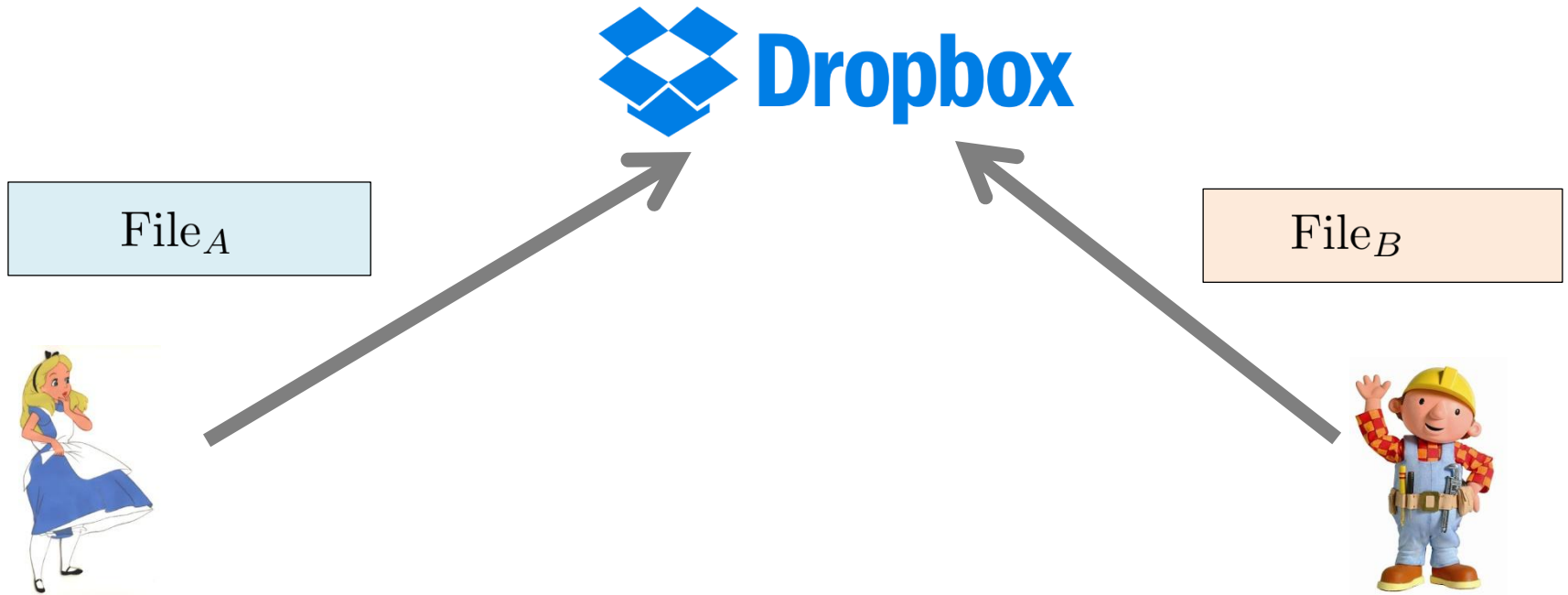
Agenda

1. Security Modeling for Hash Functions

2. Building Hash Function: MD Transform

3. Application: Password Storage

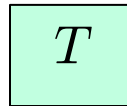
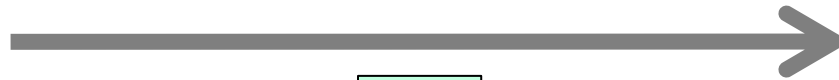
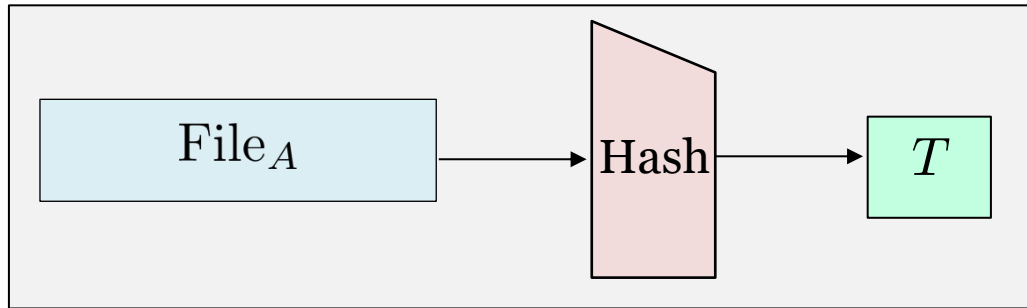
Motivating Application: Data Deduplication



Dropbox's goals:

- If many users store the same file, keep only a **single** copy
- Minimize bandwidth usage

Motivating Application: Data Deduplication



Check tags of existing files for duplication



Send / Not Send



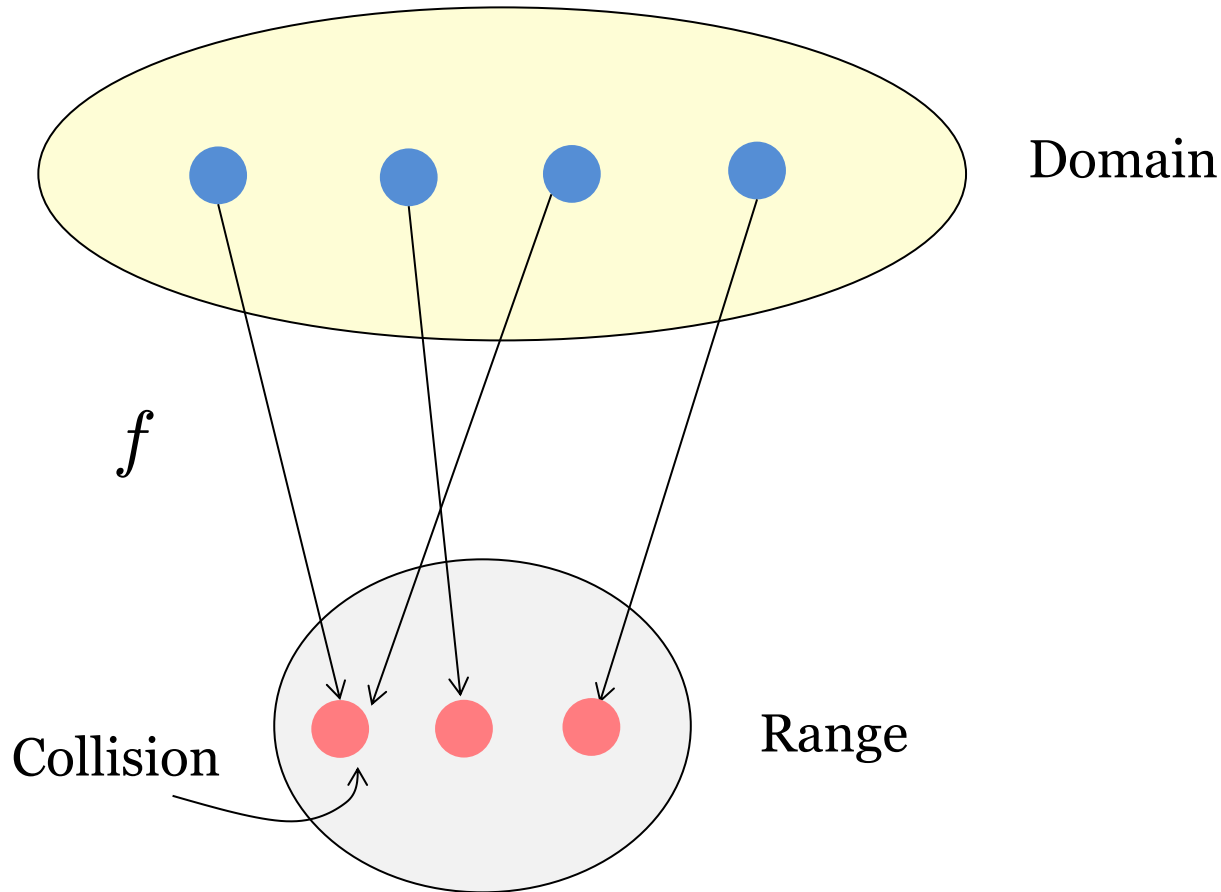
Send only when requested

What property

do we need for the hash?

Collision-Resistance

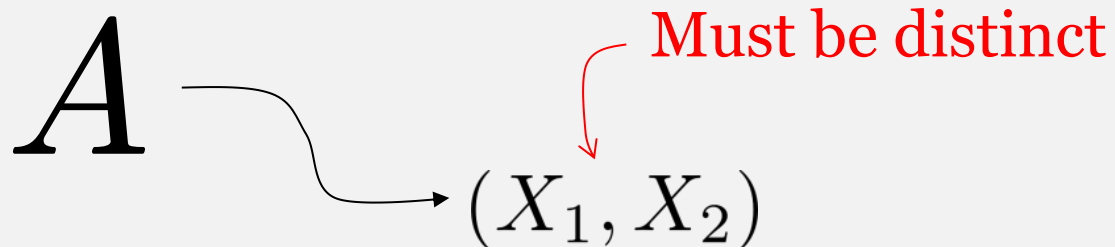
$$f : \text{Domain} \rightarrow \text{Range}$$



By Pigeonhole Principle, if $|\text{Domain}| > |\text{Range}|$ then collision exists

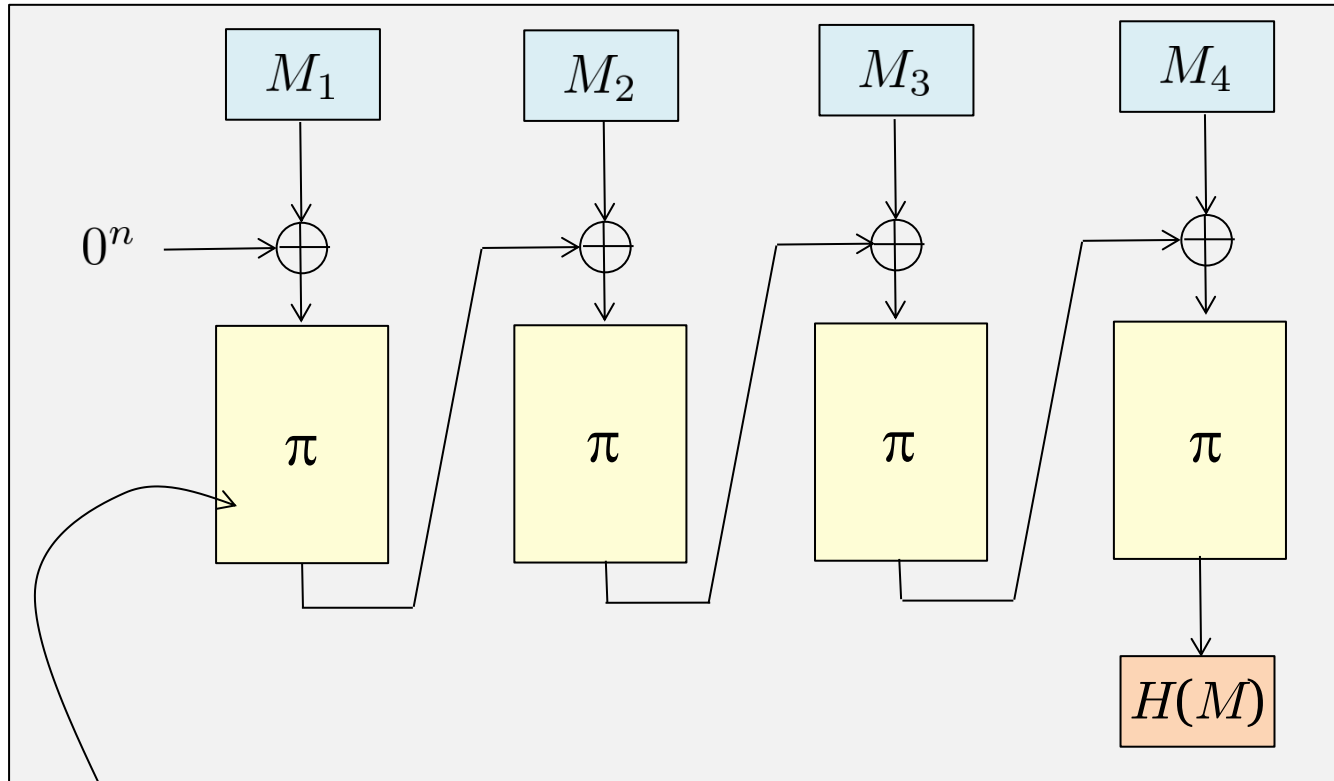
Want: collisions are hard to find, although they exist

Defining Collision-Resistance



$$\mathbf{Adv}_H^{\text{cr}}(A) = \Pr[H(X_1) = H(X_2)]$$

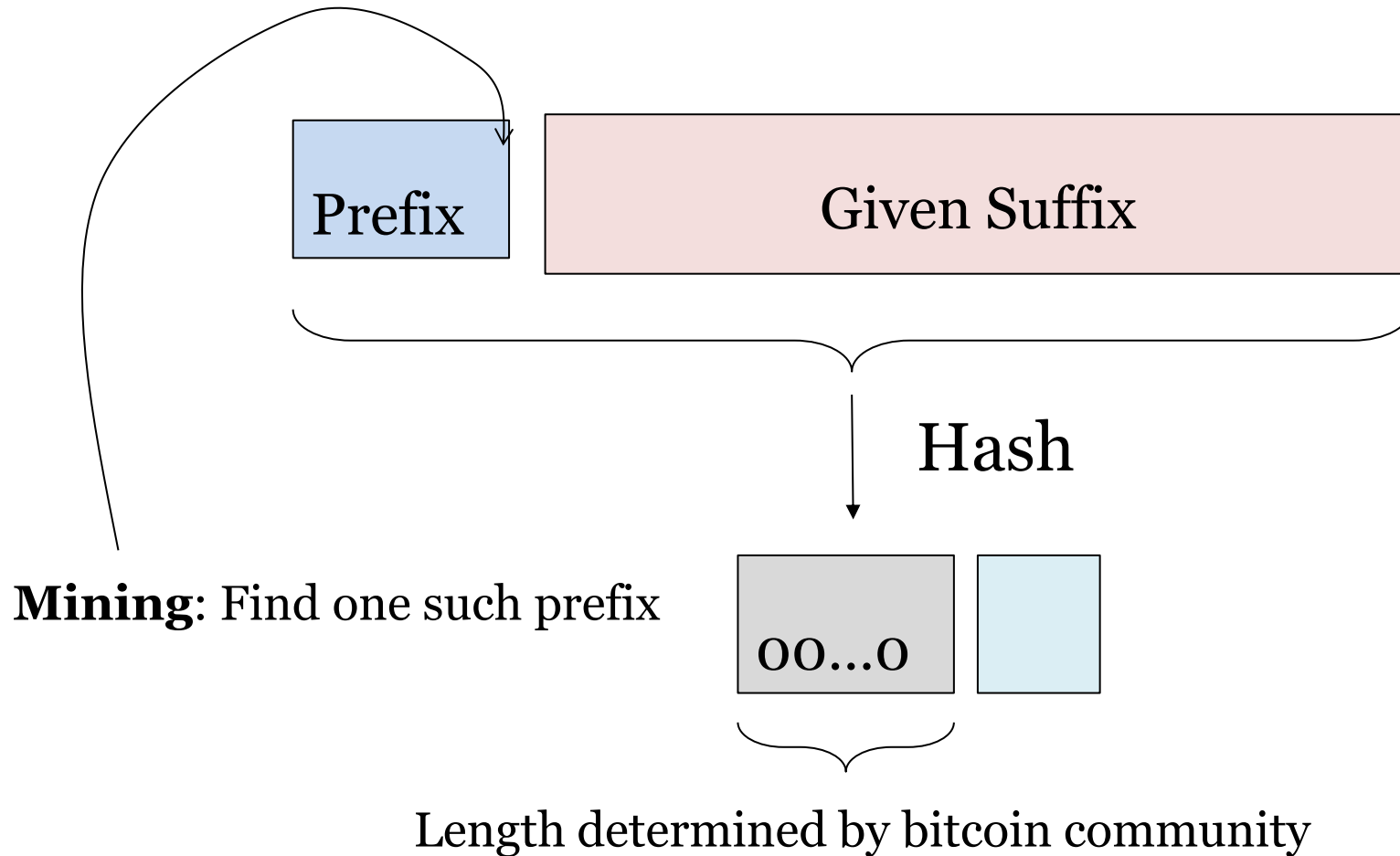
Exercise: Break Collision Resistance



π, π^{-1} are public

Public permutation

CR Is Not Enough: Bitcoin Mining



Want: Can't mine faster than brute-force

Modeling Security of Hash Functions

The Random Oracle Model

RO



Maintain a secret random $f : \{0, 1\}^n \rightarrow \{0, 1\}^m$

Everybody, including the adversary, has access to RO

Agenda

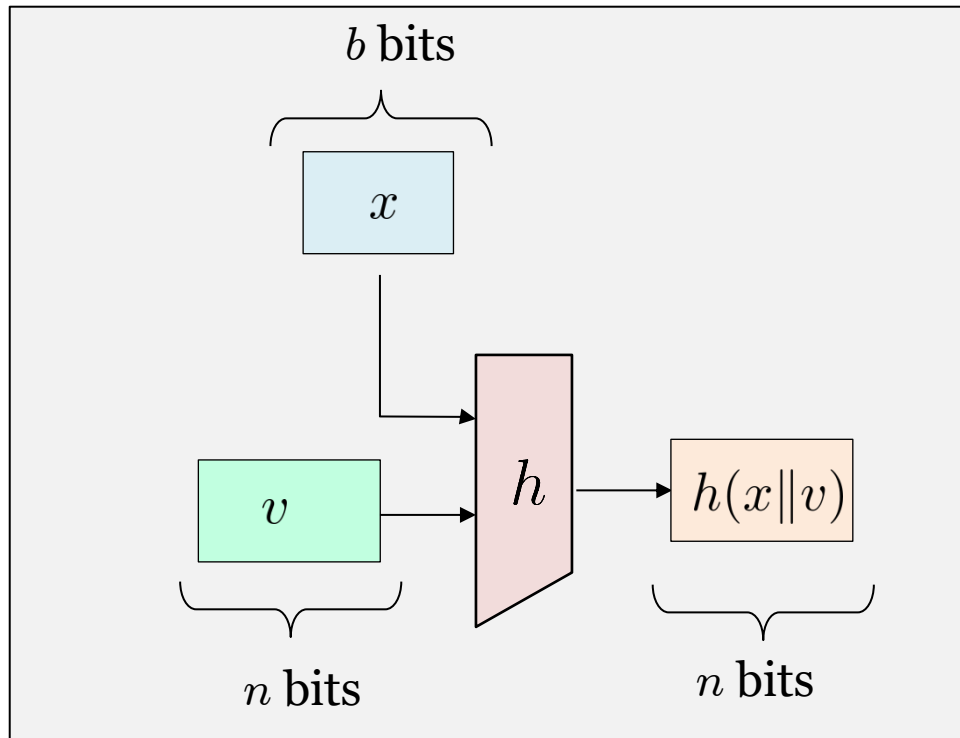
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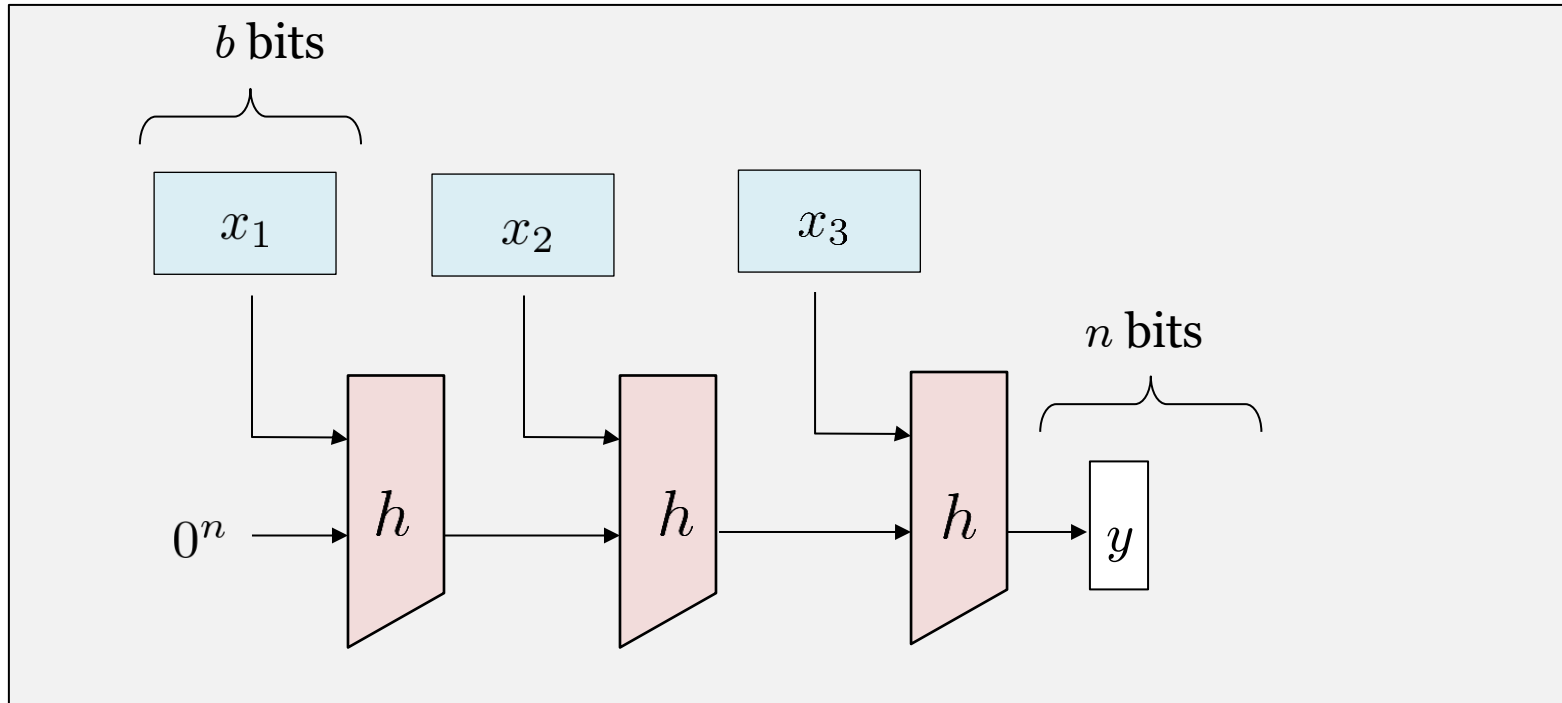
Compression Functions

$$h : \{0, 1\}^{b+n} \rightarrow \{0, 1\}^n$$



For SHA-2, $b = 512$ and $n = 256$

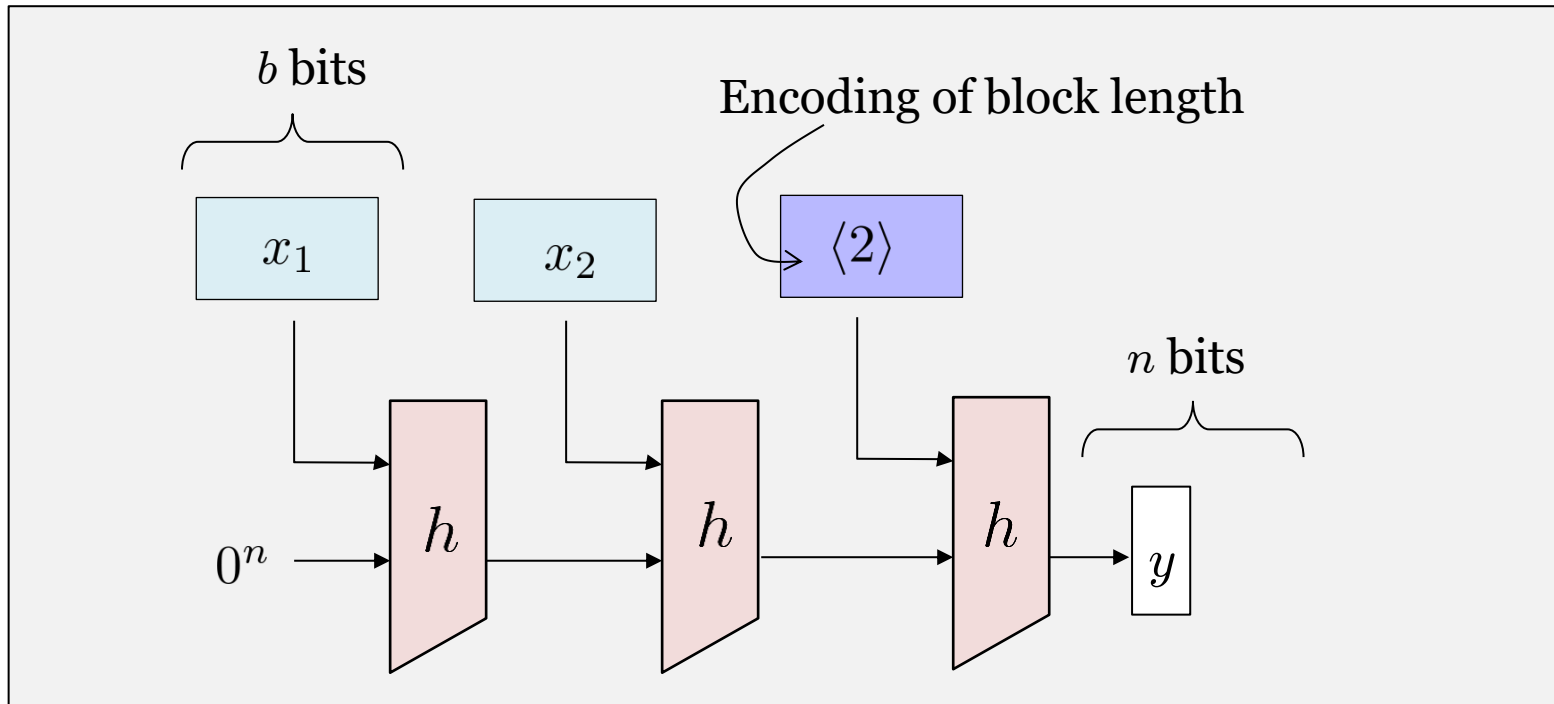
First Attempt



Question: Suppose that $h(0^b \| 0^n) = 0^n$

Break the collision resistance of H

Second Attempt: Plain Merkle-Damgard



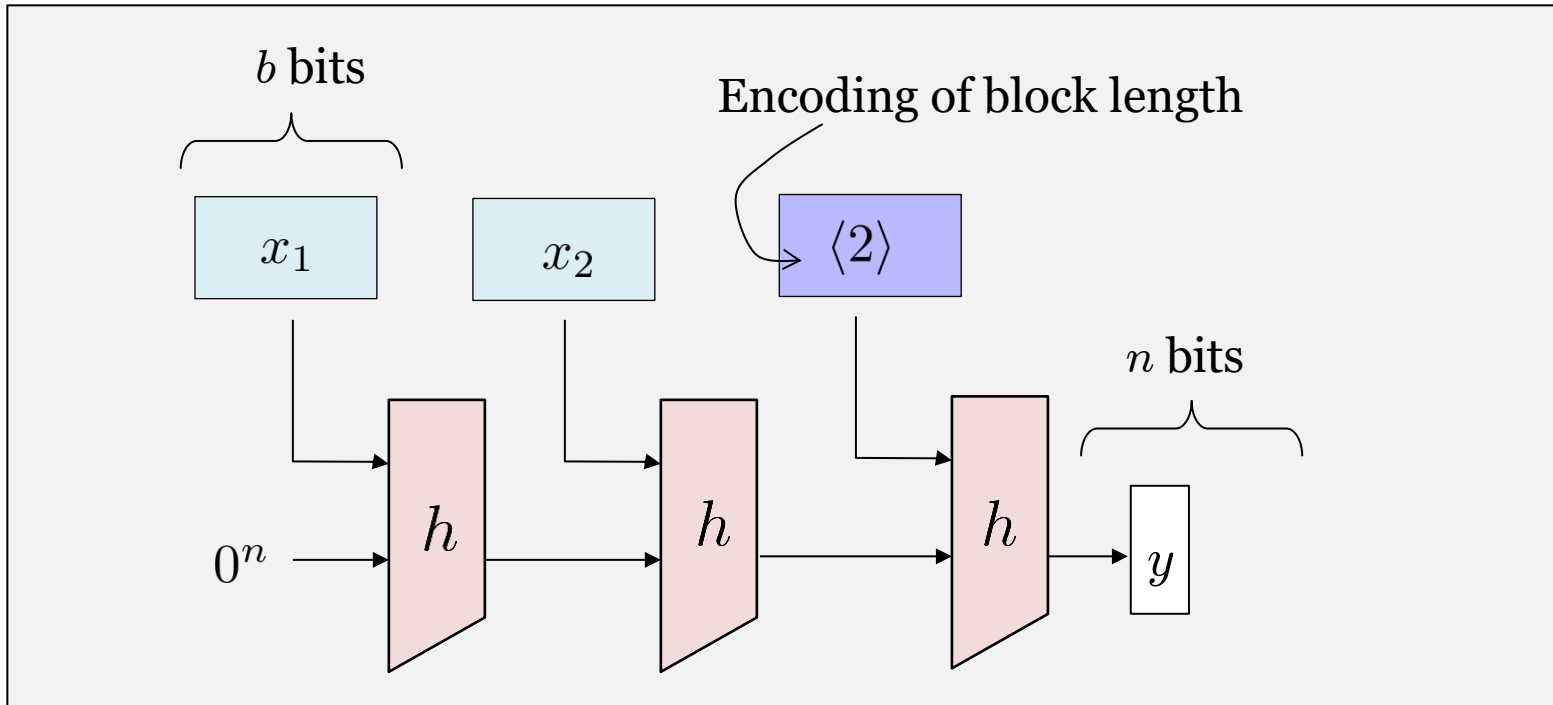
This is the structure of SHA-256

Theorem: If h is CR then $H = \mathbf{MD}(h)$ is also CR

Can't attack H if h has no weakness

Plain MD Is Not Enough for All Applications

Length-Extension Attack



Question: Consider the following MAC F

$$F_K(x) = H(K||x)$$

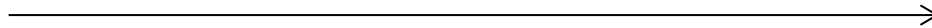
Break the MAC security of F using a single Tag query

The Damage of Length Extension Attack

Hacking Trick: Bypass Authentication



K



bank.com

K

bank.com/api?token=**ad6613c382**&user=alice&cmd=NoOp

$H(K || \text{"user=alice\&cmd=NoOp"})$

Adversary tricks Alice to perform a harmless command to learn an authentication token

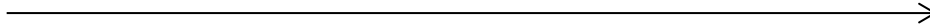


The Damage of Length Extension Attack

Hacking Trick: Bypass Authentication



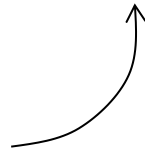
K



bank.com

K

bank.com/api?token=dbb78b593f&user=alice&cmd=NoOp&cmd=OpenSafe

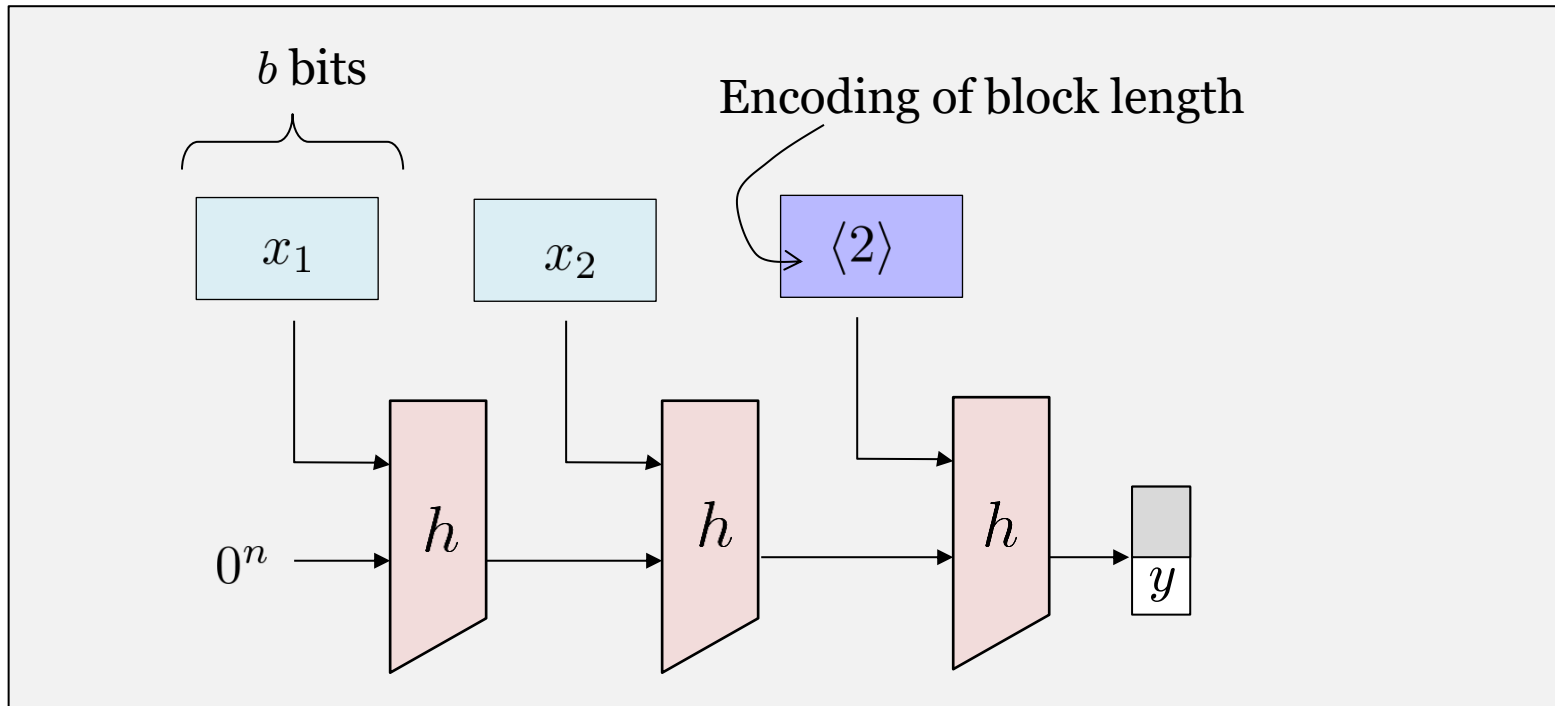


$H(K \parallel \text{"user=alice\&cmd=NoOp\&cmd=OpenSafe"})$

Adversary can compute the authentication token for a damaging command

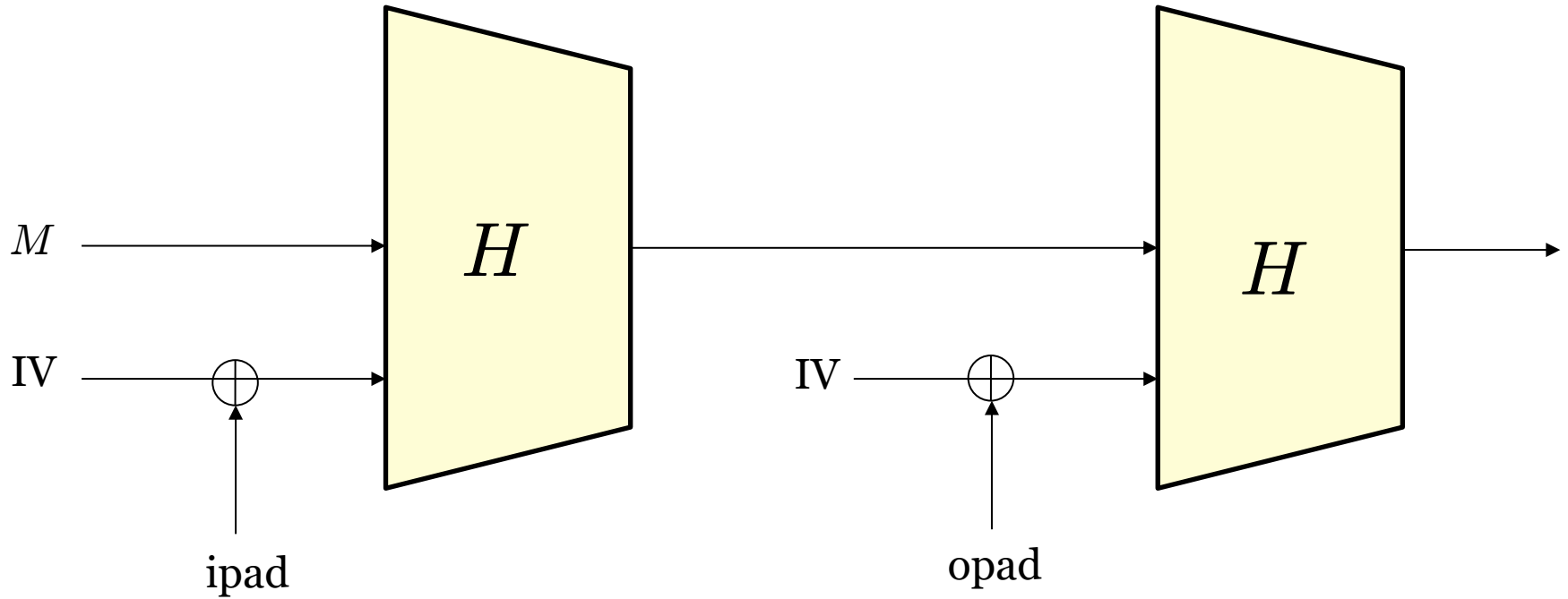


The (Strengthened) MD Transform



The output needs to be truncated

How To Have Large Output: HMAC



On large input, HMAC is only a bit more expensive than SHA-256

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Password Storage

MOTHERBOARD
TECH BY VICE

T-Mobile Stores Part of Customers' Passwords In Plaintext, Says It Has 'Amazingly Good' Security

A T-Mobile Austria customer representative's admission in a Twitter thread.

ars TECHNICA

BIZ & IT —

How an epic blunder by Adobe could strengthen hand of password crackers

Engineers flout universal taboo by *encrypting* 130 million pilfered passwords.

NEWS

Hackers crack more than 60% of breached LinkedIn passwords

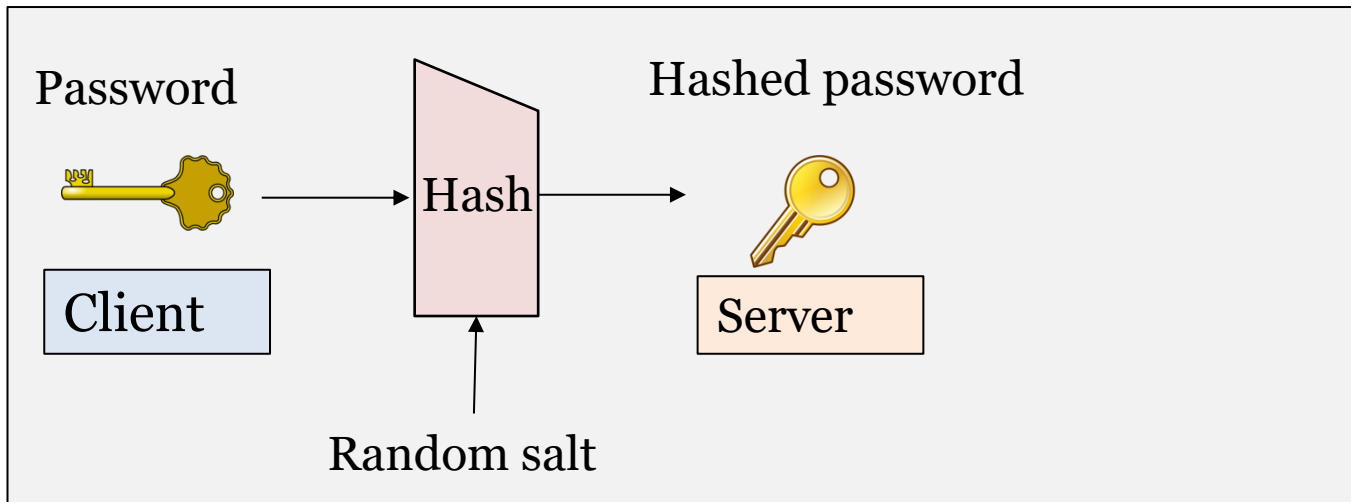
Speed of hackers to crack passwords shows weakness of security scheme used by LinkedIn, researchers say

How Should Servers Store Users' Passwords?

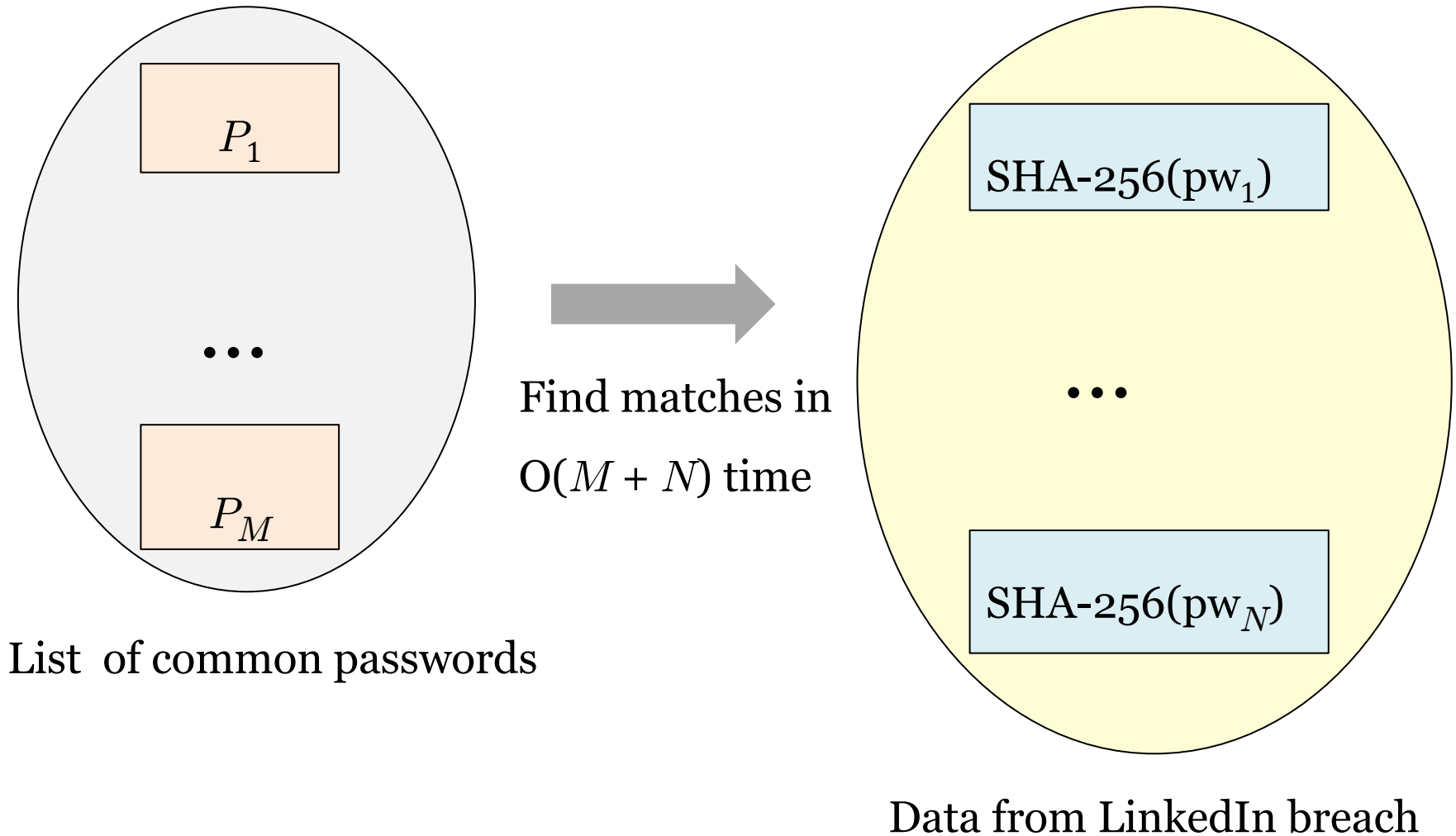
Rule 1: Only store hash outputs of passwords

Even server can't recover the passwords

Rule 2: Use a random salt for each user

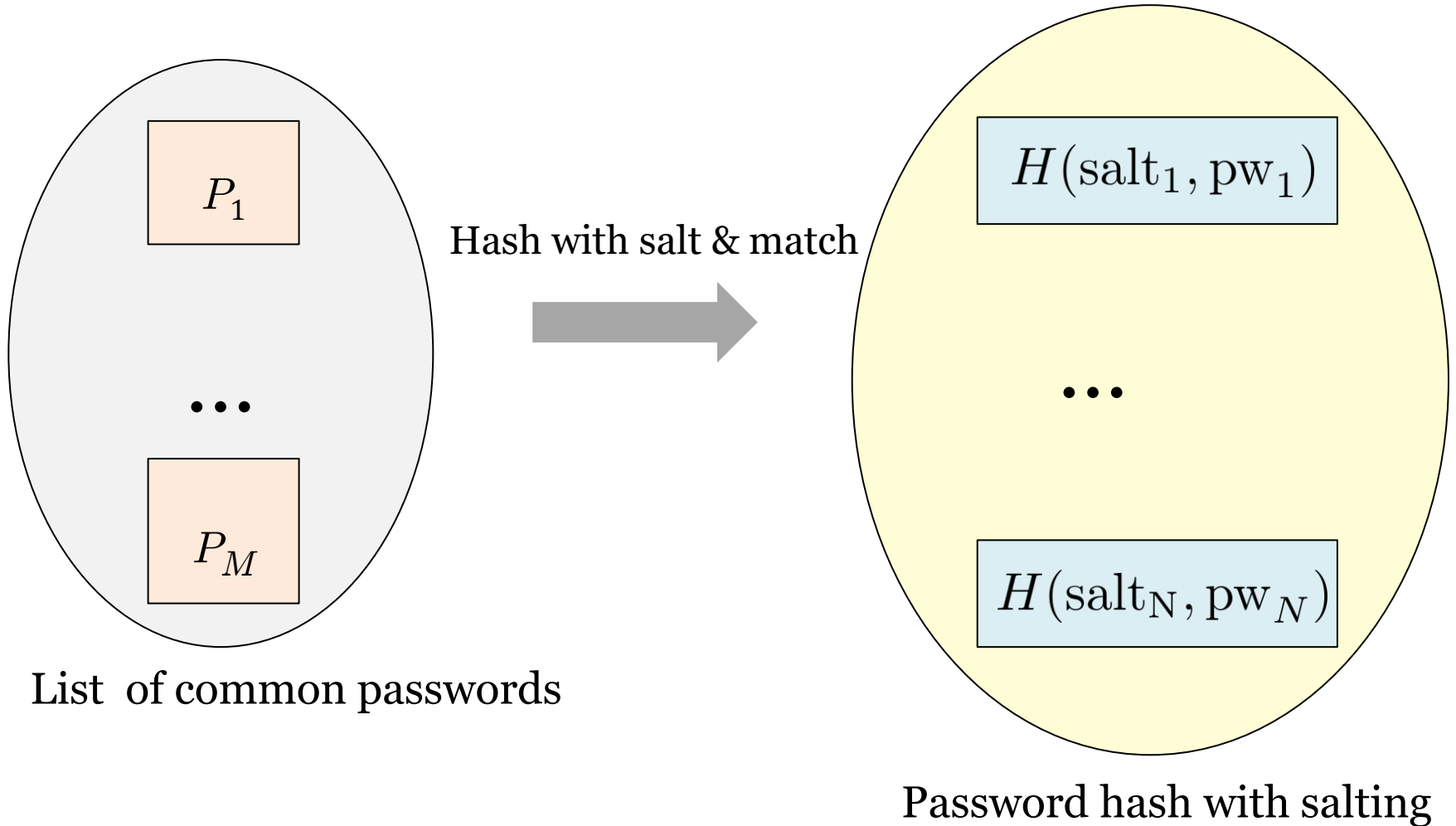


Why Salts: Dictionary Attacks



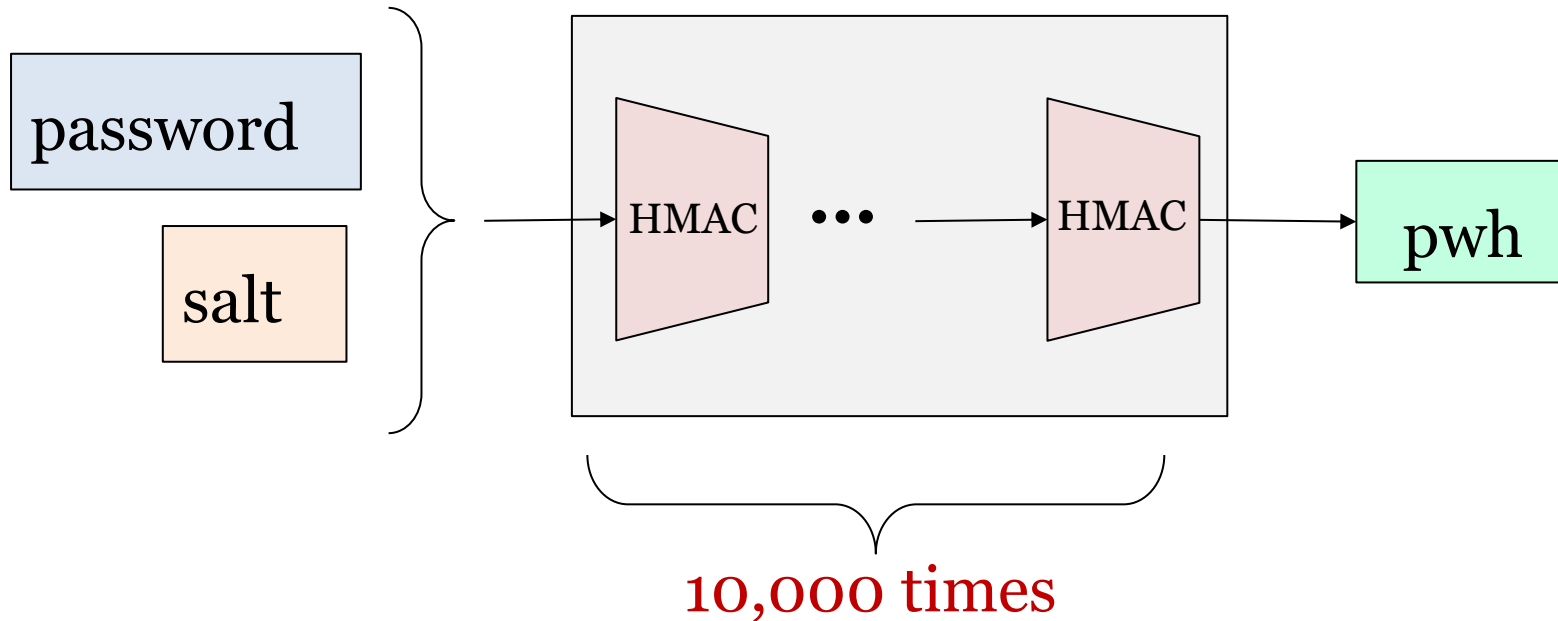
Cost of Dictionary Attacks on Salting

Need $\Theta(Mq)$ calls to H to recover q passwords



Make It Even More Expensive

Deliberately Slow Hashing



- Makes no difference for human users.
- Increase the cost of attackers for 10,000 times